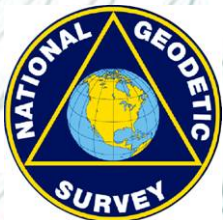


Decoding the Mystery of Coordinates

NHLSA
TOWN MONUMENT LOCATION
WORKSHOP
UNH – DURHAM, N.H.
8-11-2007

PART 1: THE DIFFERENT COORDINATE SYSTEMS



UNIVERSITY of NEW HAMPSHIRE



Decoding the Mystery of Coordinates

Objective of Presentation:

To introduce and discuss the common
Surveying and Mapping Coordinate Systems
used to establish the position of monuments

PRESENTATION OUTLINE

- 4 SURFACES
- 3 HEIGHTS
- 2 DATUMS
- 4 COORDINATE SYSTEMS
- 3 DISTANCES
- 5 NORTHS

The background features a series of parallel teal lines that are slightly curved and converge towards the left side of the frame, creating a sense of depth and perspective. The lines vary in thickness and are set against a light, off-white background.

FOUR SURFACES

FOUR SURFACES

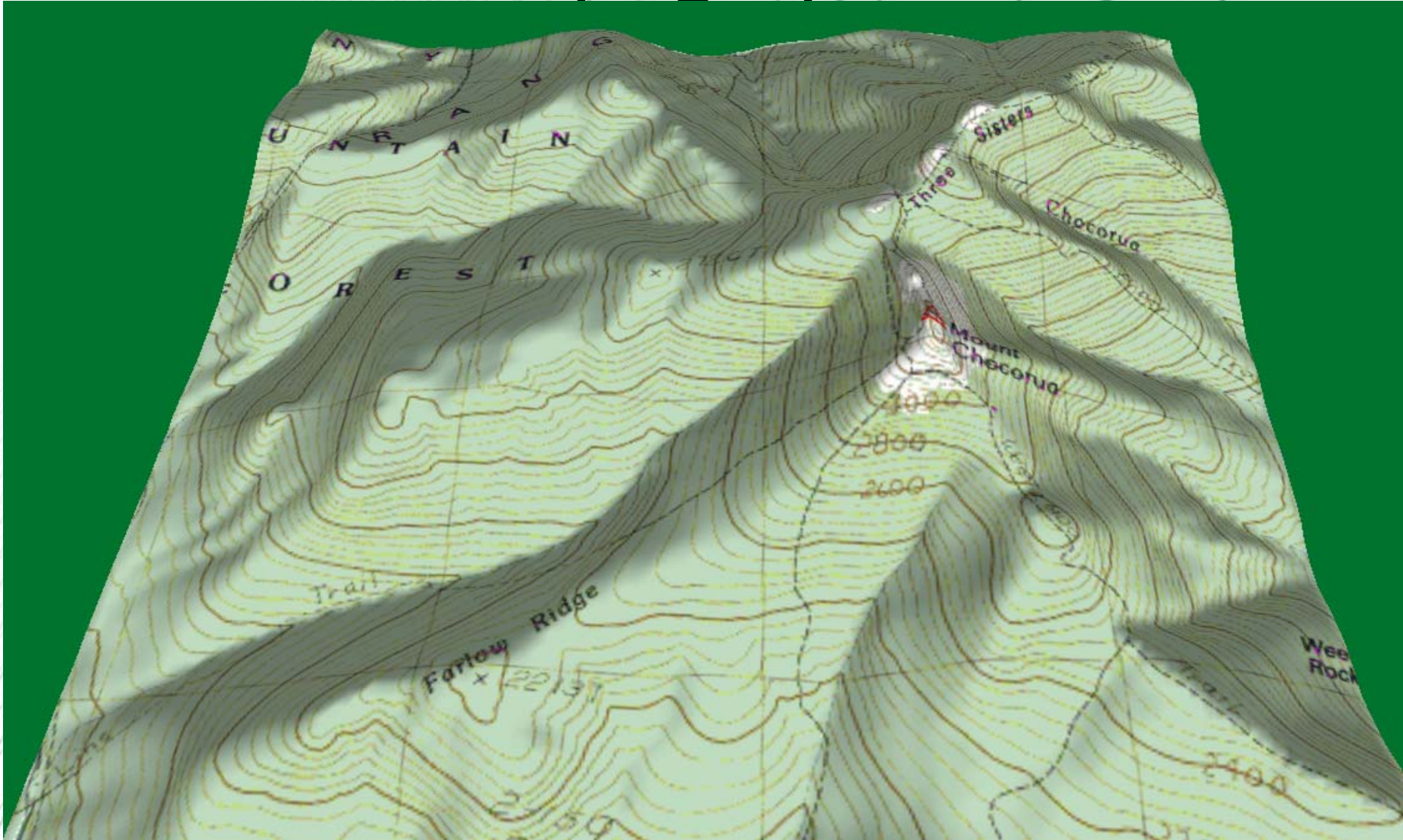
- 1- Earth - Topographic surface
- 2- Geoid - “Sea Level or “equipotential surf.
- 3- Ellipsoid - Mathematical surface
- 4- Grid - Projection, flat surface



1. Earth's Topographic Surface



1. Earth's Topographic Surface



2. Earth's "Sea Level" Surface

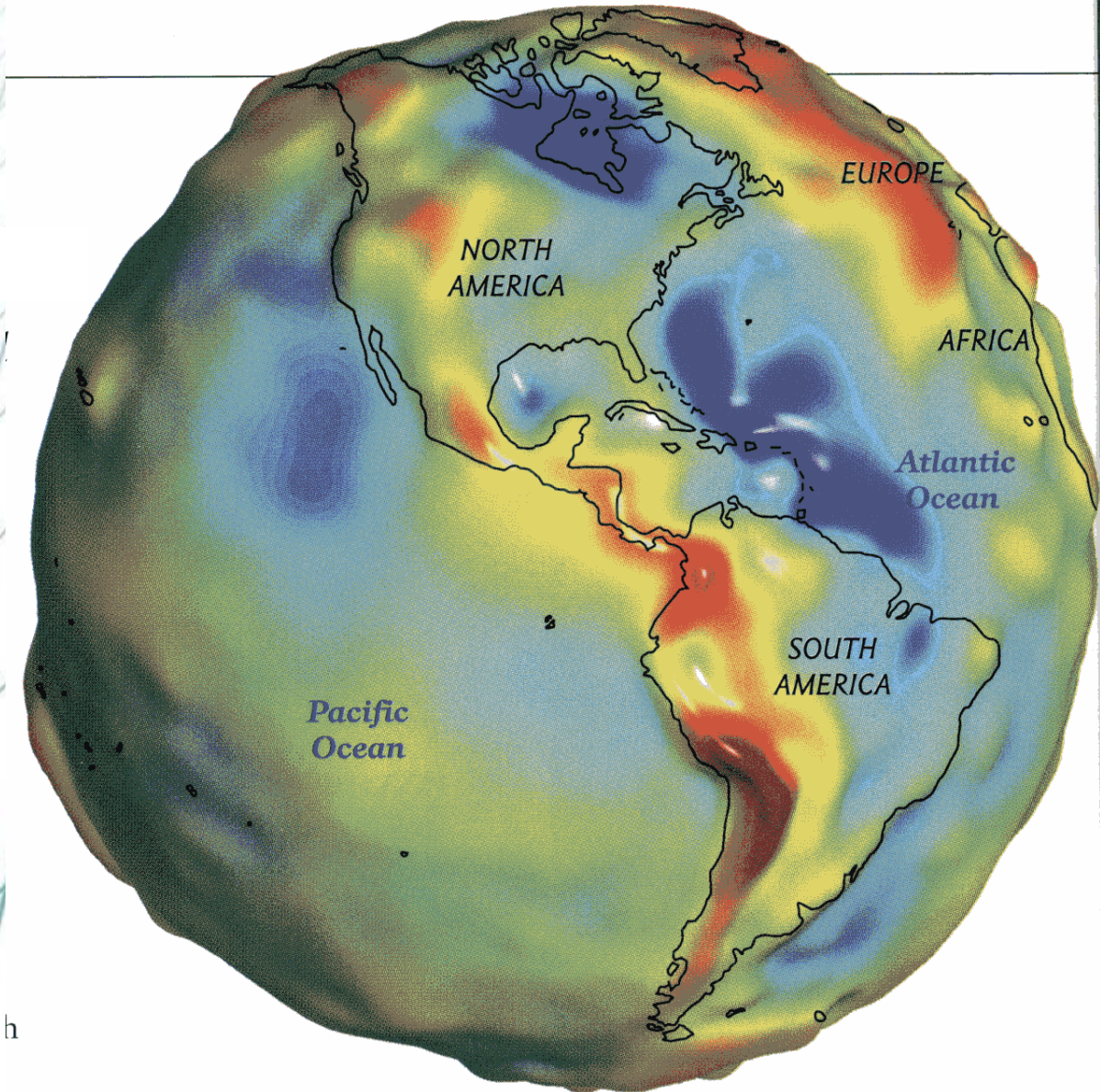
THE GEOID:

Equipotential, or
gravity surface

Current Model is
Geoid 03

Gravity Recovery
and Climate
Experiment
(GRACE)

Center for Space Research
Univ. of Texas



h

s

3. Earth's "Mathematical" Surface

THE ELLIPSOID:

World Geodetic System '84
WGS '84

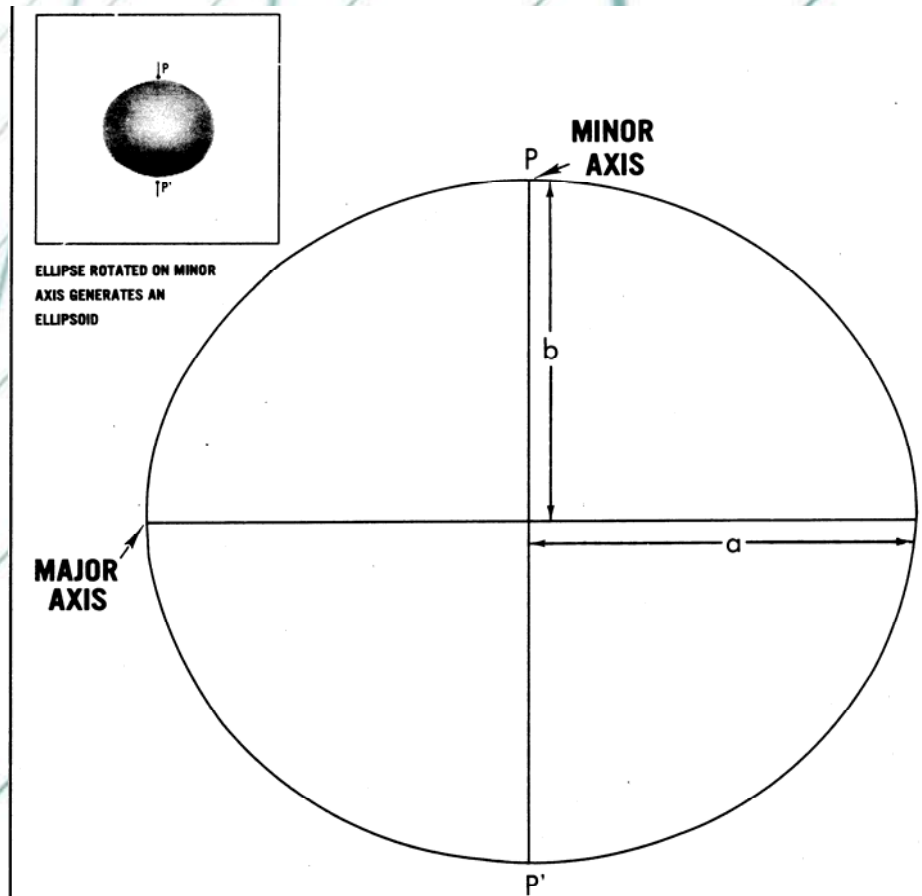
$$a = 6,378,137 \text{ meters}$$

$$b = 6,356,752.3142 \text{ meters}$$

$$f = 1 / 298.25722$$

For a circle, flattening = 0

Coordin



a = ONE-HALF OF THE MAJOR AXIS = SEMI-MAJOR AXIS

b = ONE-HALF OF THE MINOR AXIS = SEMI-MINOR AXIS

$$f = \text{FLATTENING} = \frac{a - b}{a}$$

Geodetic Coordinate Systems

A Set Of Rules For Specifying How Coordinates Are To Be Assigned To Positions On The Surface Of The Earth.
Defined BY X,Y,Z On An Ellipsoid

What We
Like To Think
The Earth Is
Shaped Like

Sphere

Equipotential
Gravimetric
Surface
(Sea-Level)

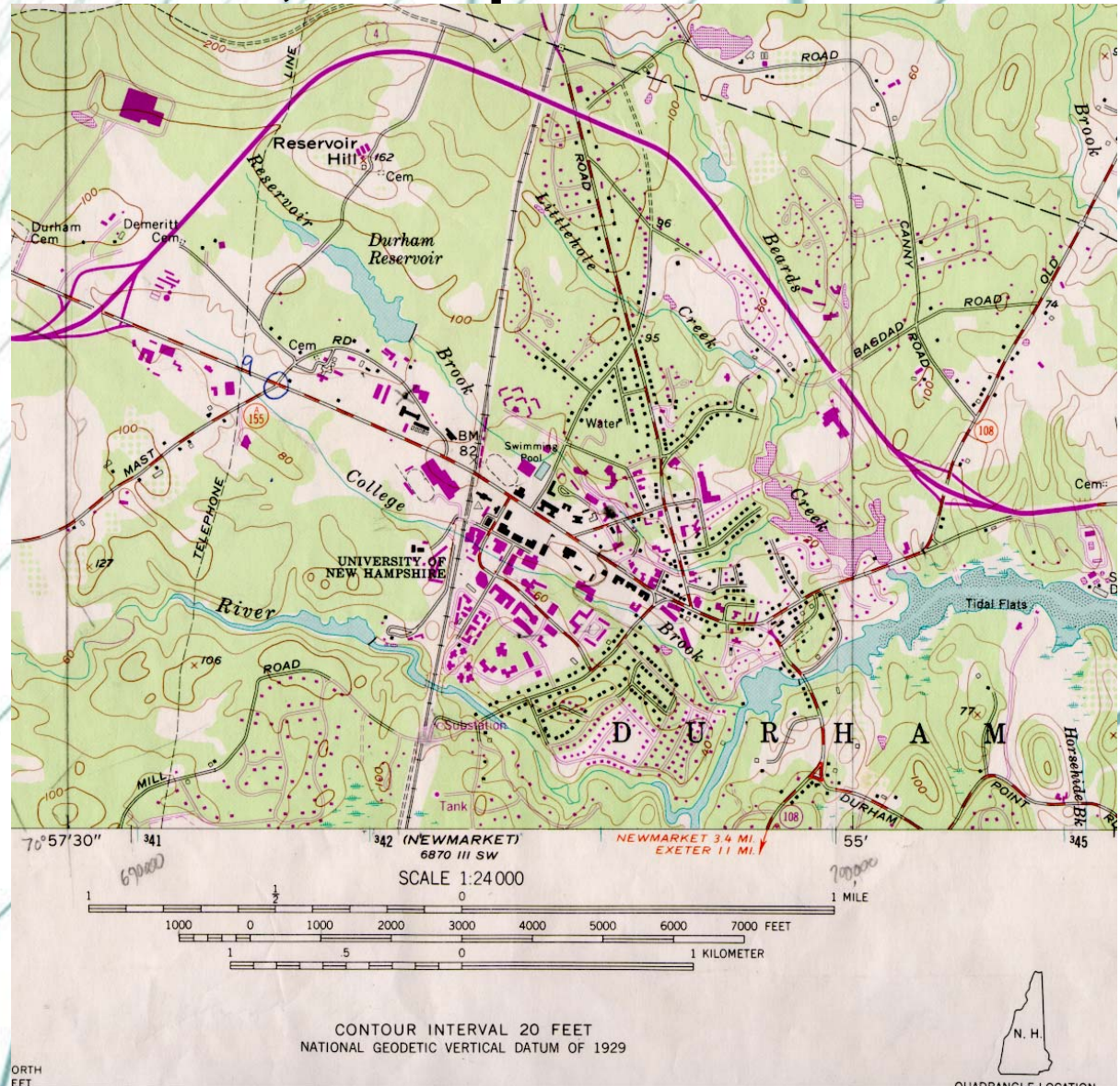
Geoid

Best Fitting Math-
ematical Shape

Ellipsoid

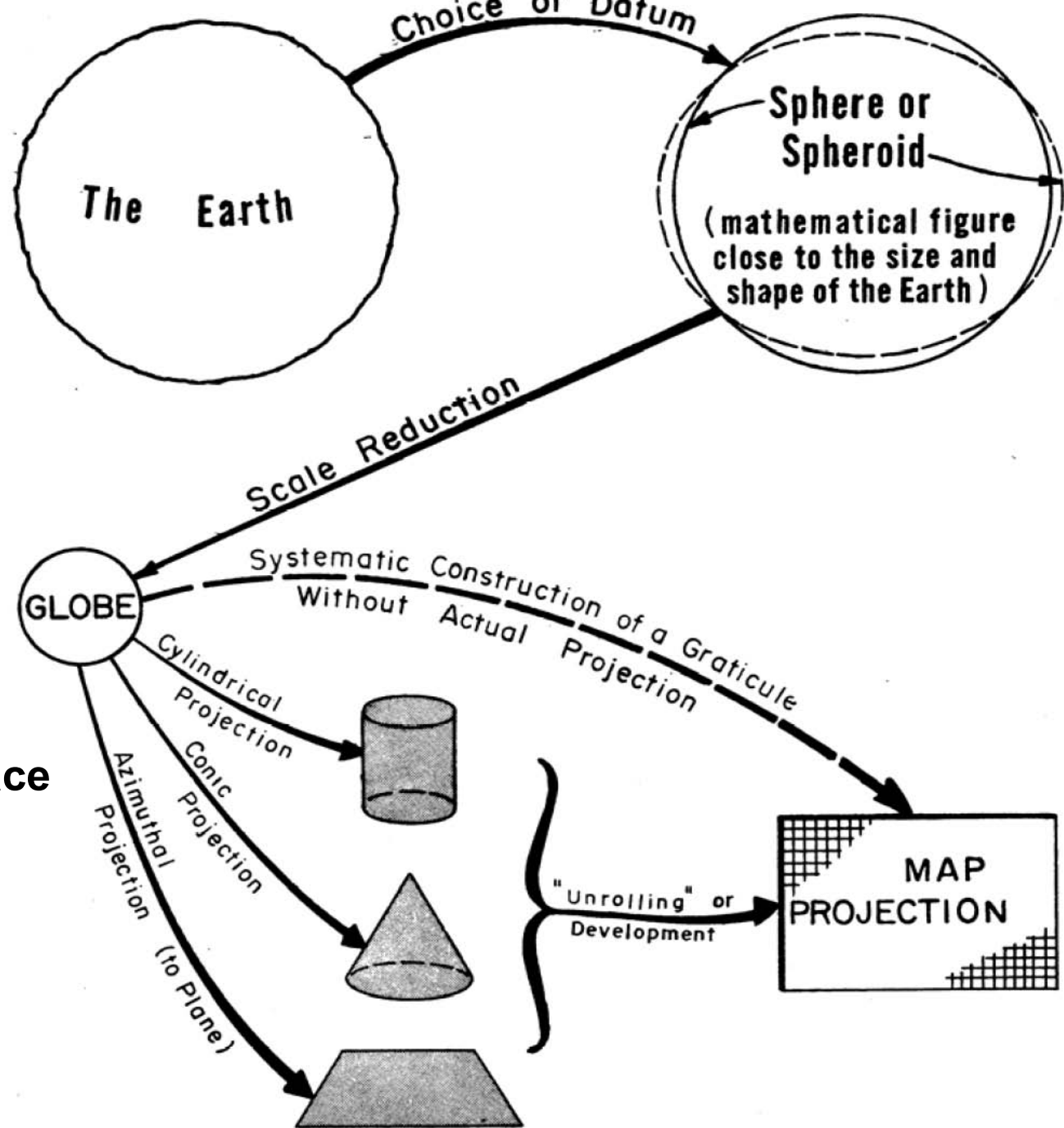
4. Earth's "Flat, Map" Surface

THE GRID



Creating The GRID:

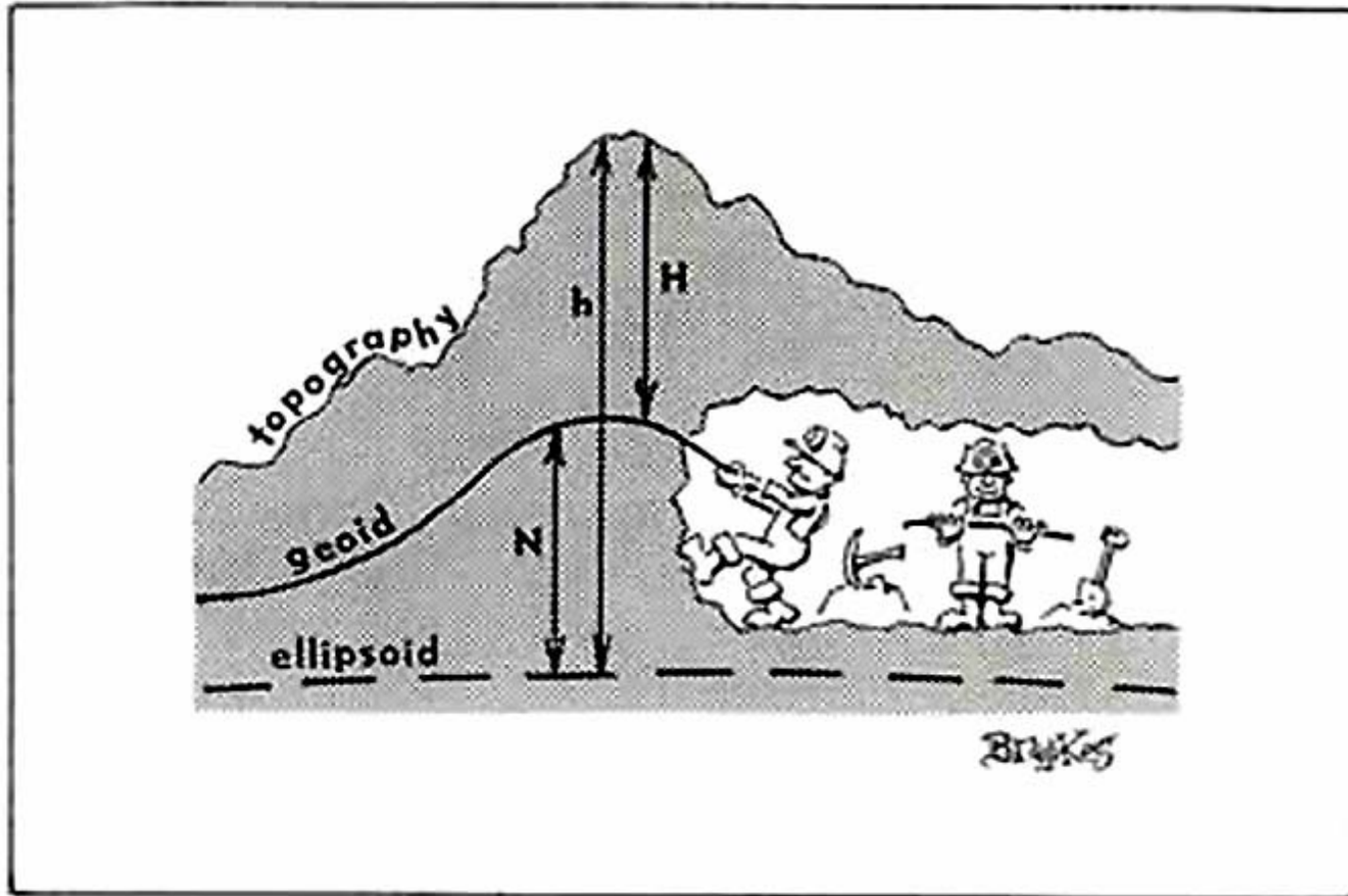
- 1 A Mathematical Surface
- 2 Reduce the Scale
- 3 Project on a surface
- 4 Unroll the surface



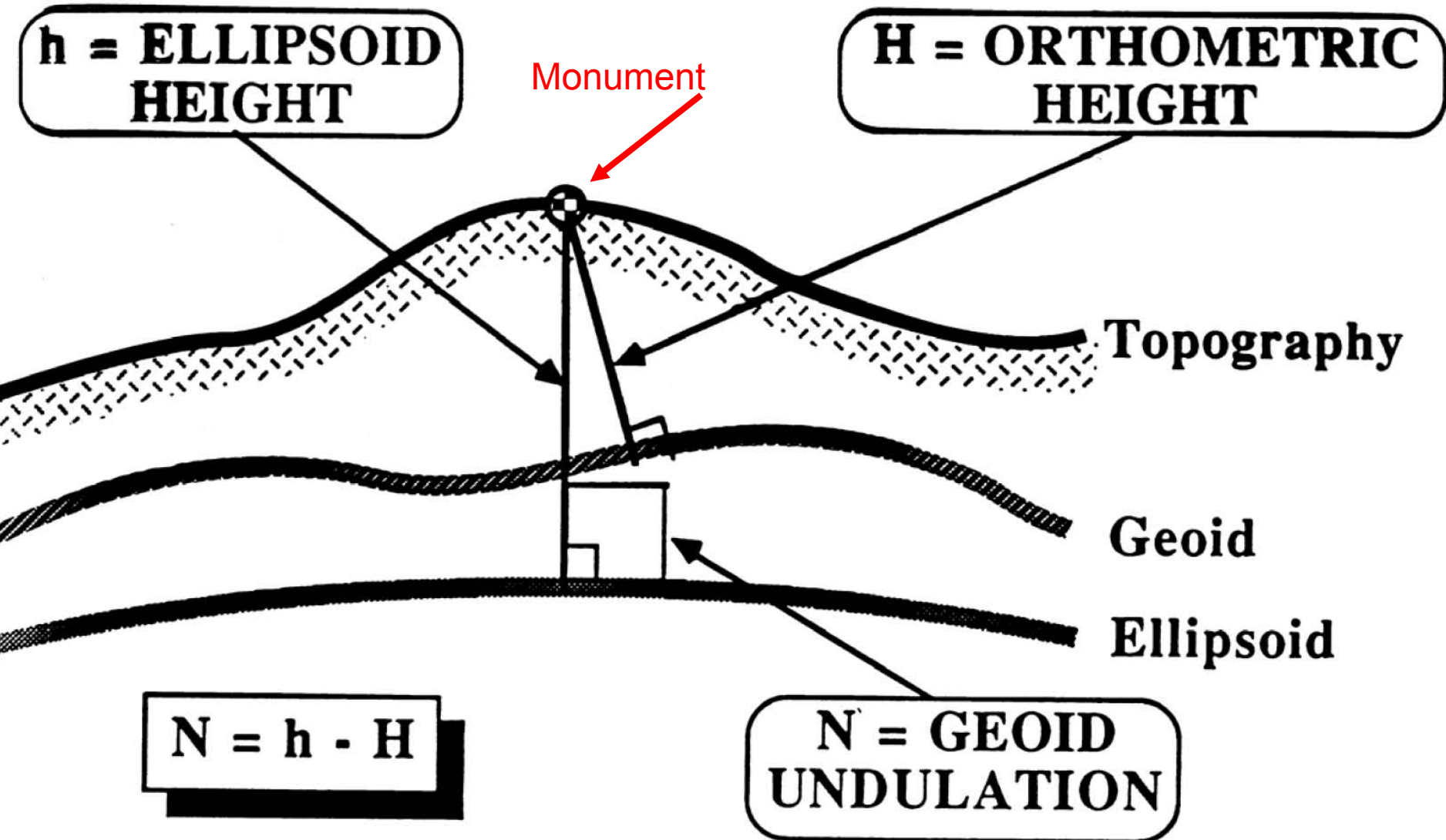


THREE “HEIGHTS”

In Search of the Geoid...



THREE "HEIGHTS"



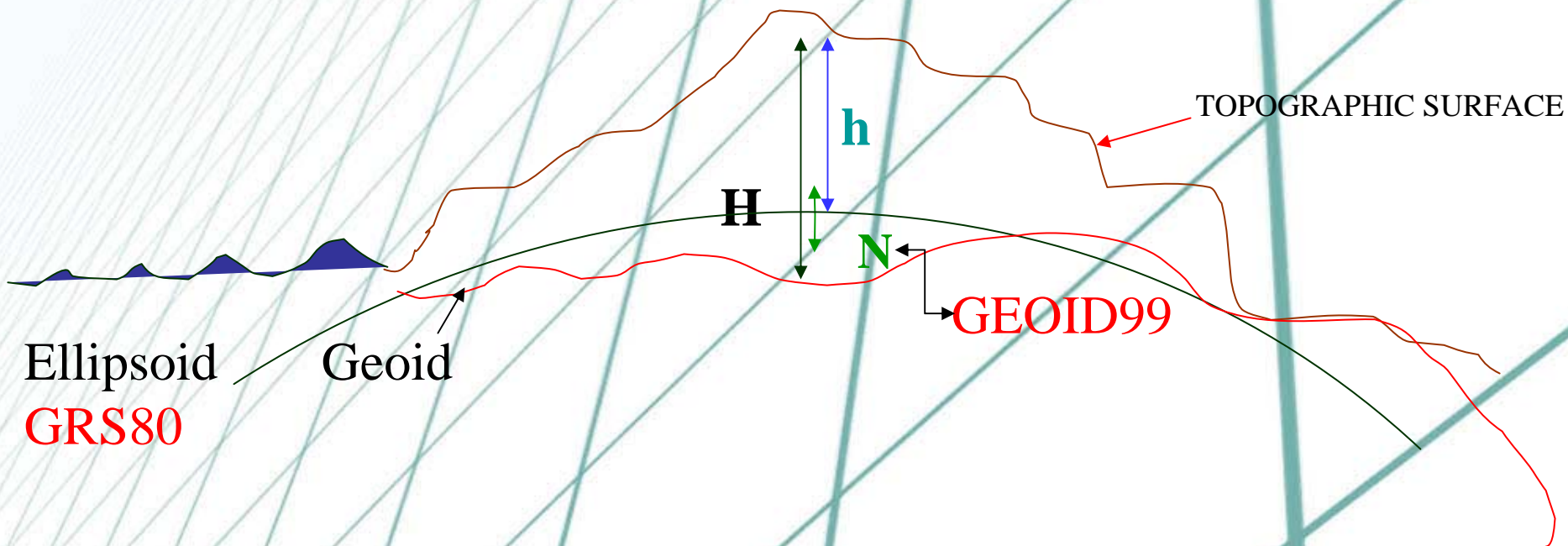
Ellipsoid, Geoid, and Orthometric Heights

H = Orthometric Height (NAVD 88)

h = Ellipsoidal Height (NAD 83)

N = Geoid Height (GEOID 03)

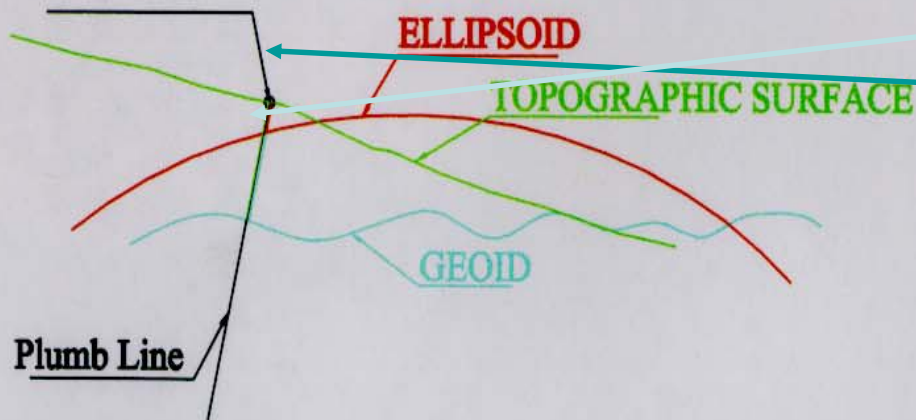
$$h = H + N$$



Ellipsoid, Geoid, and Orthometric Heights

STATION "DURHAM 1943" : Has **THREE** "Heights"

Station "Durham 1943"



Station "Durham 1943"

Orthometric Height = 106.46'

Geoid Height = -89.19'

Ellipsoid Height = +17.27'

Ellipsoid Height = Orthometric Height + Geoid Height

$$h = H + N$$

$$17.27' = 106.46' + -89.19'$$

TWO DATUMS

TWO DATUMS

A Datum:

Any numerical or geometrical quantity or set of such quantities which serve as a reference or base for calculation of other quantities. (GMS)

1. Horizontal Geodetic Datum: An Ellipsoid
2. Vertical Geodetic Datum: “Mean Sea Level” ≈ Geoid

What is a GEODETIC DATUM?

- Geodetic Datum
 - “A set of constants specifying the coordinate system used for geodetic control, i.e., for calculating coordinates of points on the Earth”*
 - “[above] together with the coordinate system and the set of all points and lines whose coordinates, lengths, and directions have been determined by measurement or calculation.”*

*Definitions from the Geodetic Glossary, September 1986

Not To Be Confused With:

- Ellipsoid

- “A closed surface, whose planar sections are either ellipsoids or circles.”*
- Mathematical figure which helps define a Reference Frame
- Clarke 1866, GRS80

- Reference Frame

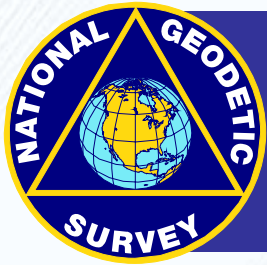
- “A coordinate system associated with a physical system.”*
- NSRS, ITRF

*Definitions from the Geodetic Glossary, September 1986

1. Horizontal Control Datum

- “A Geodetic Datum specifying the coordinate system in which horizontal control points are located.”
- Defined by 8 Constants
 - 3 – specify the location of the origin of the coordinate system.
 - 3 – specify the orientation of the coordinate system.
 - 2 – specify the dimensions of the reference ellipsoid.
- NAD 27, NAD 83

*Definition from the Geodetic Glossary, September 1986



UNITED STATES ELLIPSOID DEFINITIONS

BESSEL 1841

$$a = 6,377,397.155 \text{ m} \quad 1/f = 299.1528128$$

$$f = (a-b)/a$$

CLARKE 1866

$$a = 6,378,206.4 \text{ m} \quad 1/f = 294.97869821$$

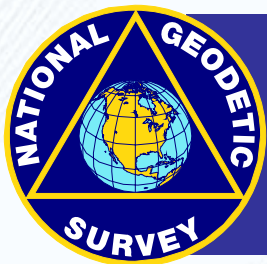
GEODETTIC REFERENCE SYSTEM 1980 - (GRS 80)

$$a = 6,378,137 \text{ m} \quad 1/f = 298.257222101$$

WORLD GEODETTIC SYSTEM 1984 - (WGS 84)

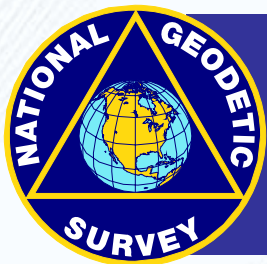
$$a = 6,378,137 \text{ m} \quad 1/f = 298.257223563$$



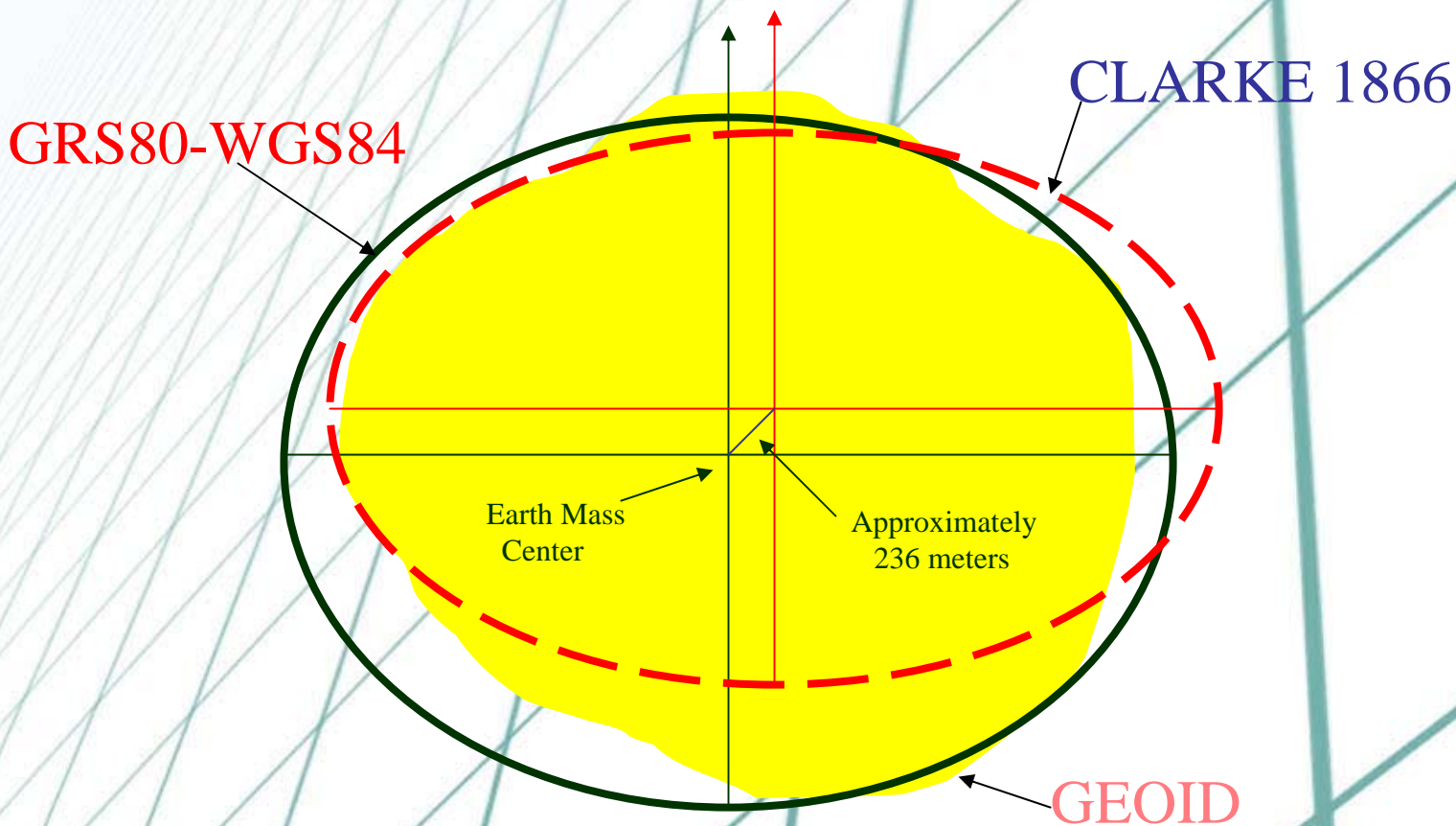


HORIZONTAL DATUMS





THE GEOID AND TWO ELLIPSOIDS



Comparison of Horizontal Datum Elements

NAD 27

NAD 83

ELLIPSOID

CLARKE 1866

$a = 6,378,206.4 \text{ m}$

$1/f = 294.9786982$

GRS80

$a = 6,378,137. \text{ M}$

$1/f = 298.257222101$

DATUM POINT

Triangulation Station
MEADES RANCH, KANSAS

NONE
EARTH MASS CENTER

ADJUSTMENT

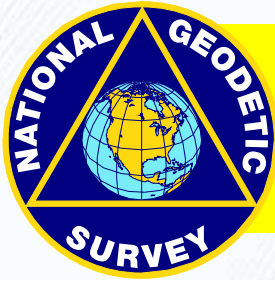
25k STATIONS
Several Hundred Base Lines
Several Hundred Astro Azimuths

250k STATIONS
Appox. 30k EDM Base Lines
5k Astro Azimuths
Doppler Point Positions
VLBI Vectors

BEST FITTING

North America

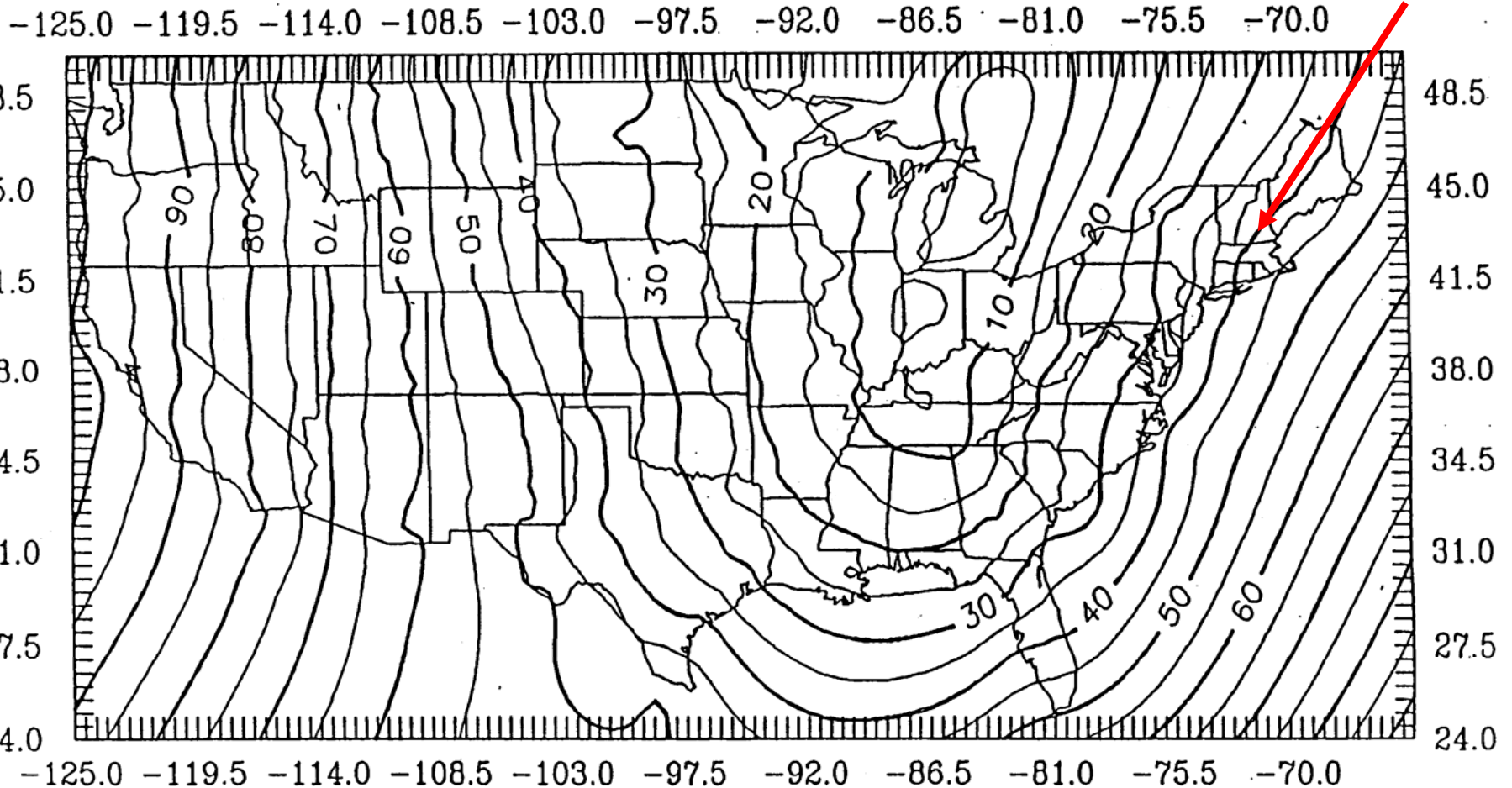
World-Wide



NAD 27 and NAD 83

MAGNITUDE OF DATUM SHIFT (METERS)

'83 Position ~ 40 meters ((131 ft.) SW of '27 position



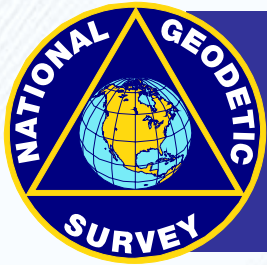
2. Vertical Control Datum

A set of fundamental elevations to which other elevations are referred

Vertical Control Datum

- “A Geodetic Datum specifying the system in which vertical control points are located.”
- A set of fundamental elevations to which other elevations are referred
- NGVD 29, NAVD 88 – Orthometric, “Sea Level”
- Others – Cairo, Local Tidal

*Definitions from the Geodetic Glossary, September 1986



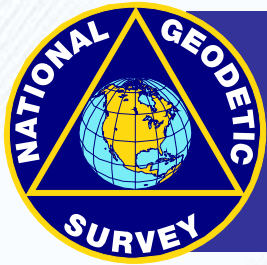
VERTICAL DATUMS

MEAN SEA LEVEL DATUM OF 1929

NATIONAL GEODETIC VERTICAL DATUM OF 1929
(As of July 2, 1973)

NORTH AMERICAN VERTICAL DATUM OF 1988
(As of June 24, 1993)





COMPARISON OF VERTICAL DATUM ELEMENTS

NGVD 29

NAVD 88

DATUM DEFINITION

26 TIDE GAUGES
IN THE U.S. & CANADA

FATHER'S POINT/RIMOUSKI
QUEBEC, CANADA

BENCH MARKS

100,000

450,000

LEVELING (Km)

102,724

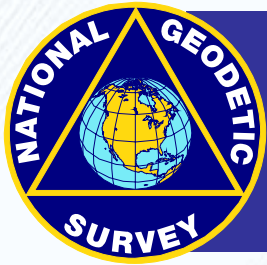
1,001,500

GEOID FITTING

Distorted to Fit MSL Gauges

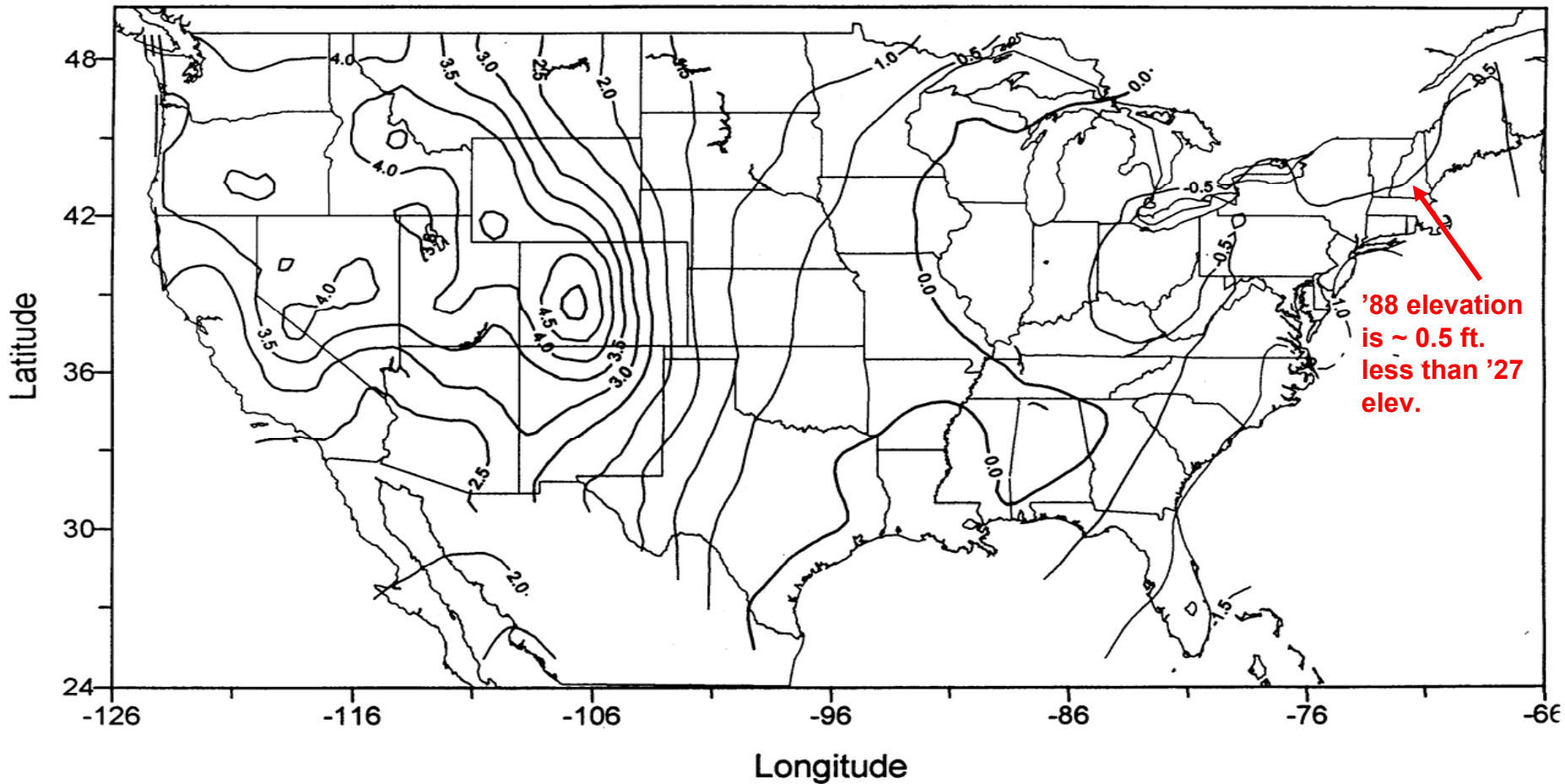
Best Continental Model





NGVD 29 and NAVD 88

NAVD88 - NGVD29 (feet)





FOUR COORDINATE SYSTEMS

FOUR COORDINATE SYSTEMS (3D)

1. GEOCENTRIC COORDINATES:

X,Y,Z

2. GEODETIC COORDINATES

Φ , λ ,h

3. CARTESIAN (PLANE) COORDINATES

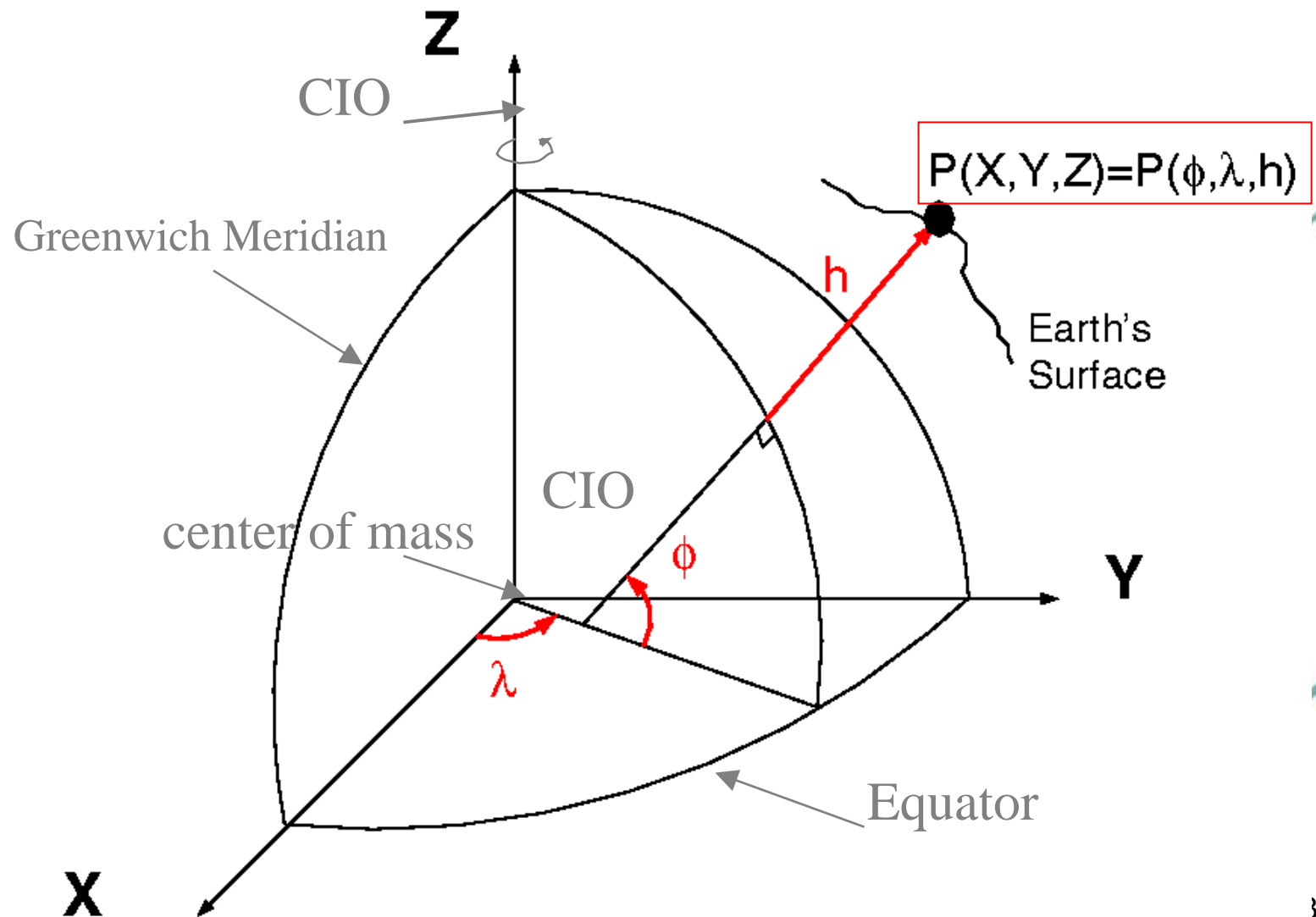
N,E,H (State Plane Coordinates., UTM coord.)

4. ASSUMED COORDINATES

Y, X, Elevation

1. Geocentric Coordinates

Conventional Terrestrial System (CTS)



1. Geocentric Coordinates (Ctd.)

- Conventional Terrestrial Reference System (CTRS) also called
- Earth Centered Earth Fixed System (ECEF) requires a
- Reference Frame (set of reference station coordinates)
one is
- International Terrestrial Reference Frame of WGS 1984

1. Geocentric Coordinates (Ctd.)

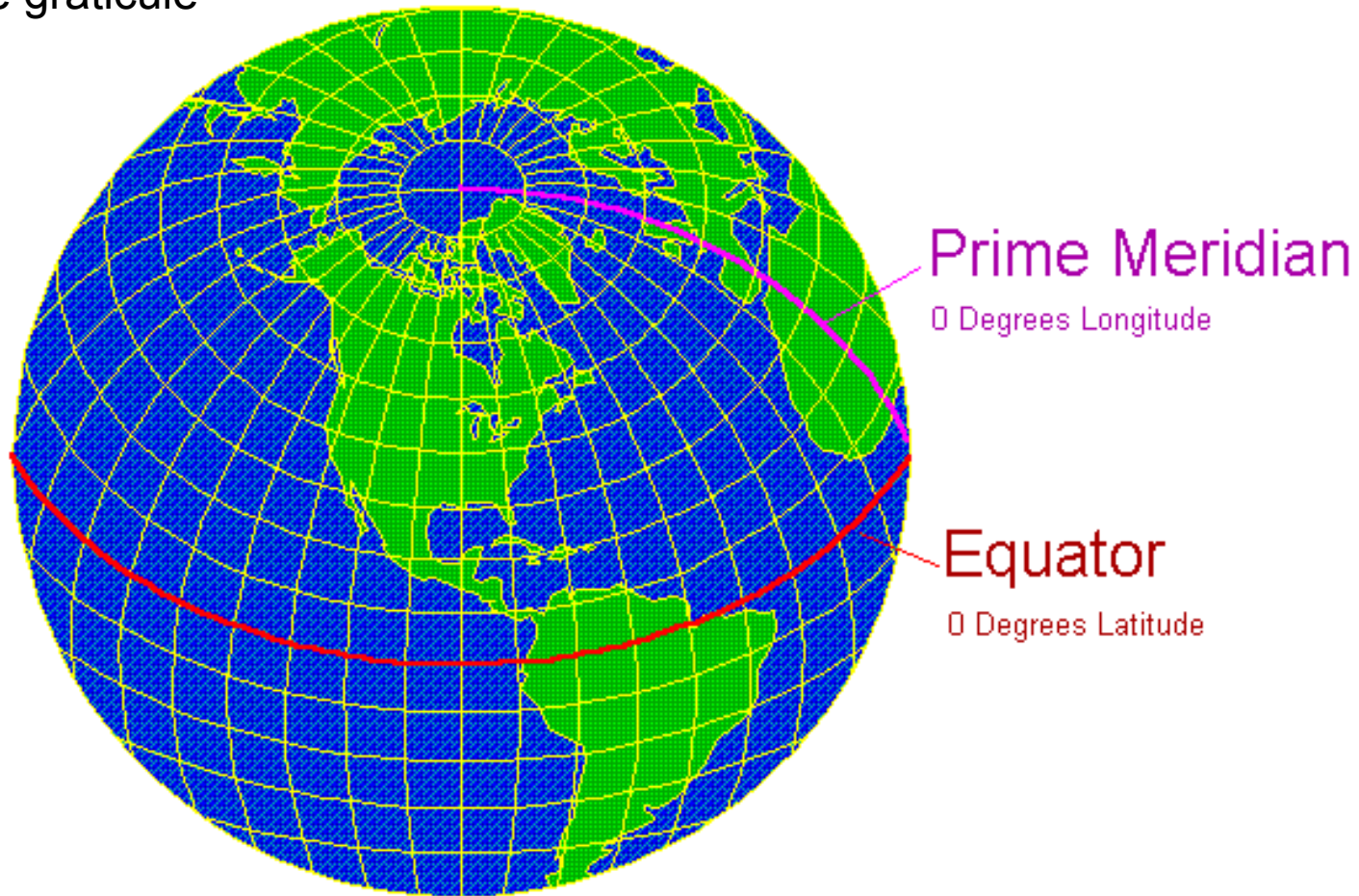
- ITRF
 - Origin at center of mass of the earth
 - Z axis passes through the International Reference Pole (IRP) as defined by the International Earth Rotation Service (IERS)
 - X axis through point of zero Longitude (on plane of conventional equator)
 - Y Axis formed by a right-handed coordinate frame and passes close to the Greenwich Meridian

2. Geodetic Coordinates

- LATITUDE: ϕ (PHI)
- LONGITUDE: λ (LAMBDA)
- Ellipsoid Height: h

2. Geodetic Coordinates

The graticule

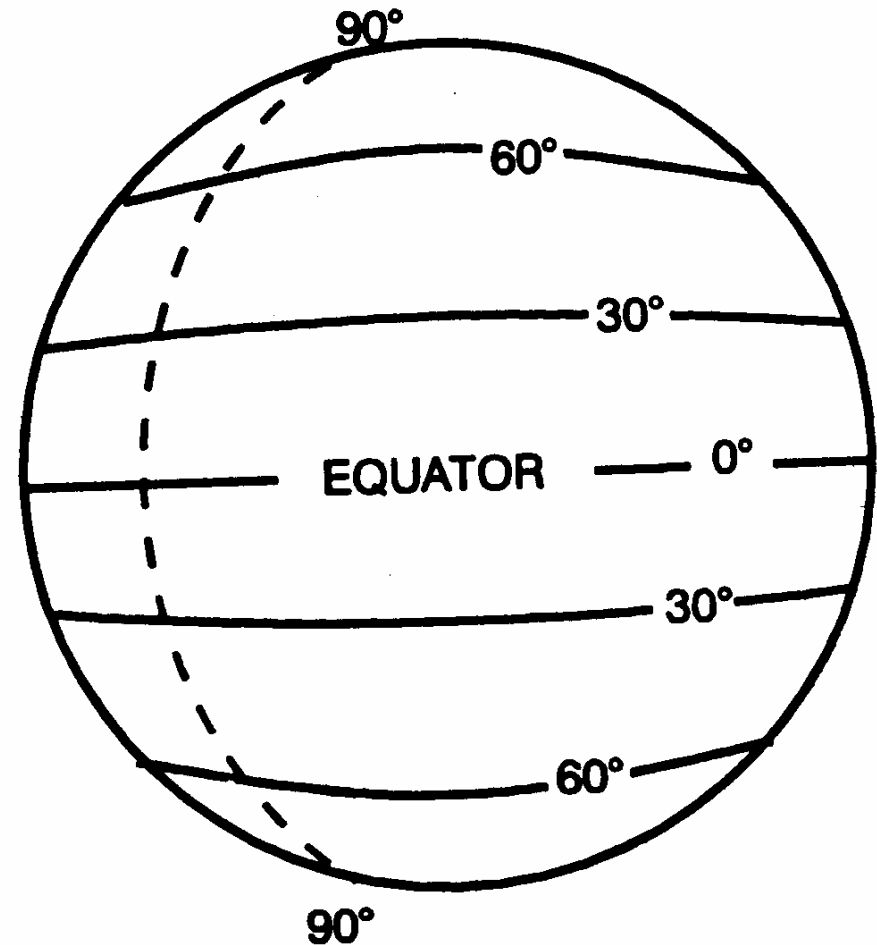


2. Geodetic Coordinates

- **LATITUDE: ϕ**

The north-south position on the Globe

“A Parallel”

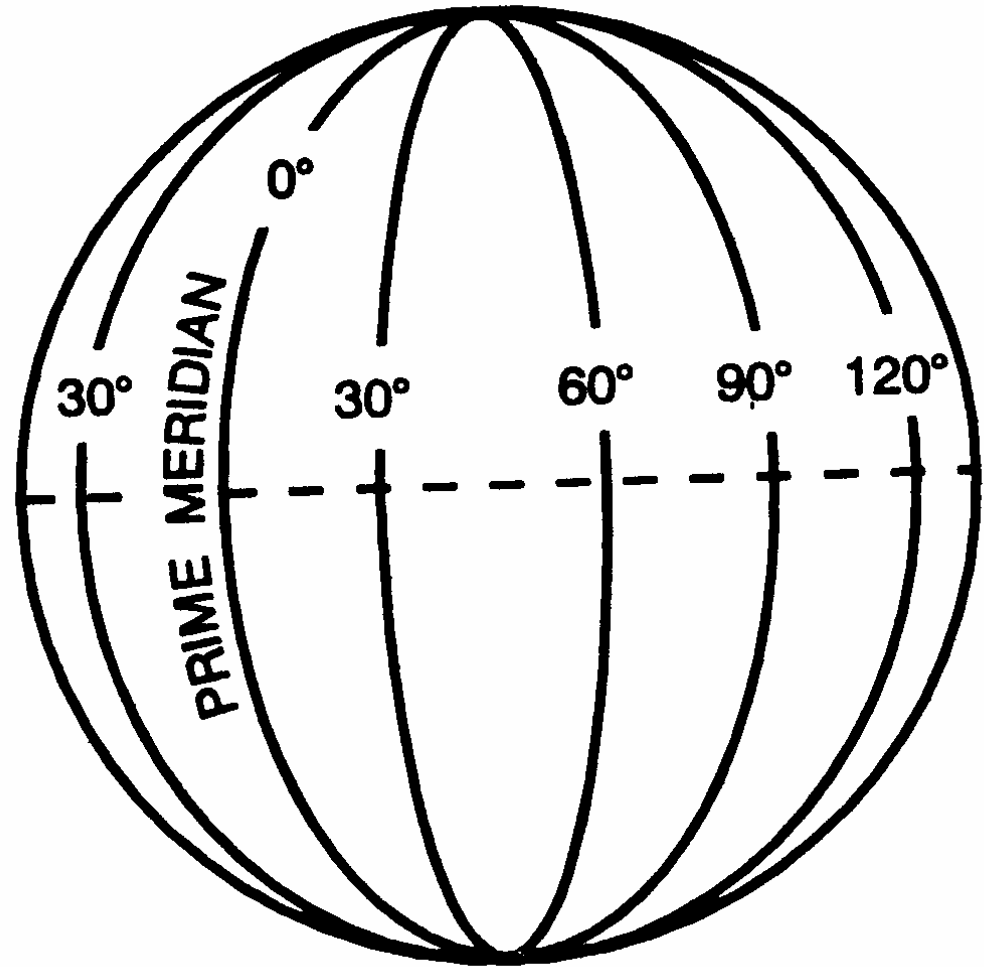


2. Geodetic Coordinates

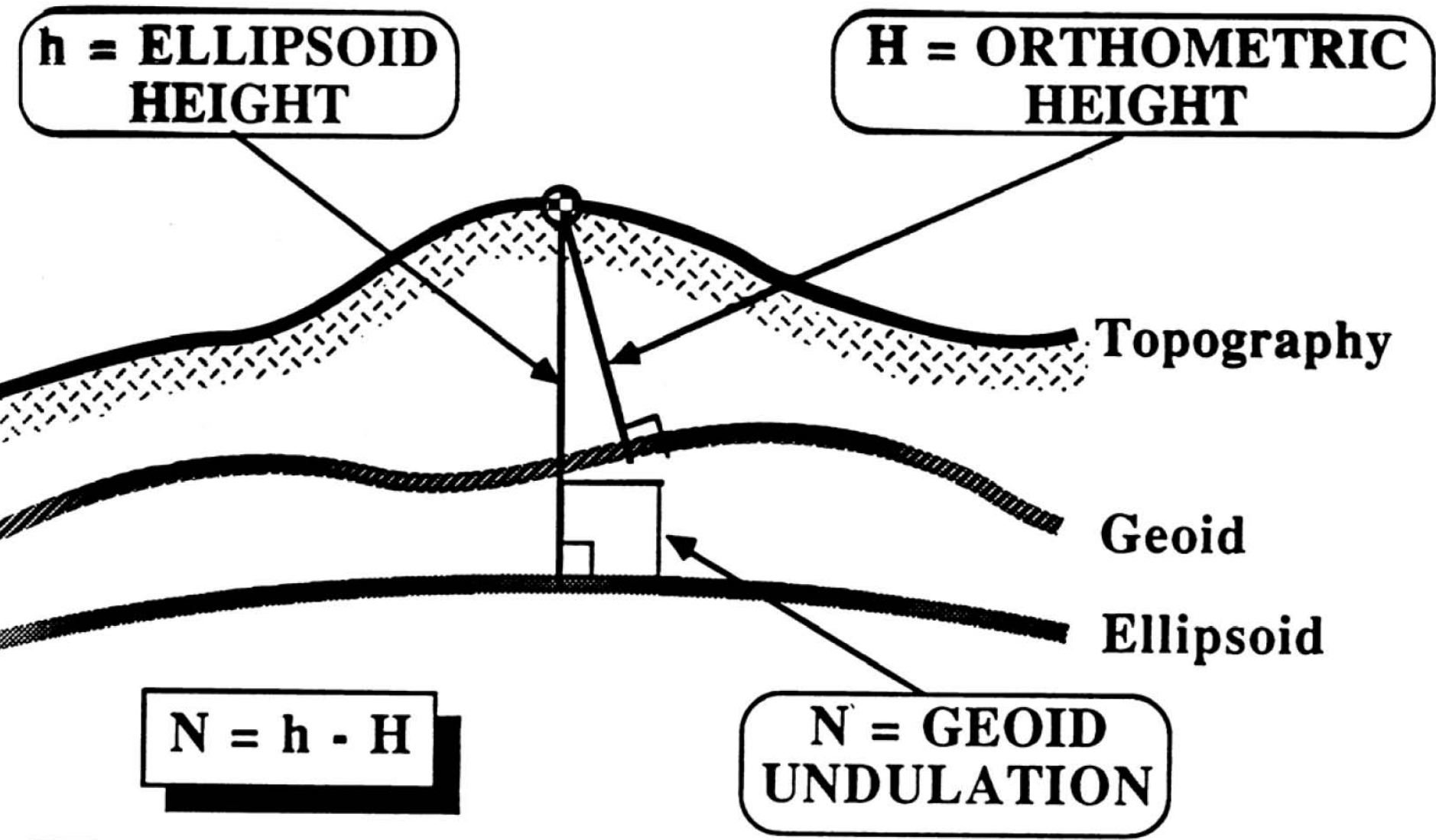
- **LONGITUDE: λ**

The east - west position on the Globe

“A Meridian”



Remember Ellipsoid Height (h)?



3. CARTESIAN (PLANE) COORDINATES

- **STATE PLANE COORDINATES (SPC):**
 - Transverse Mercator States
 - Lambert Conformal States
 - 2 Issues
 - Convergence/Mapping Angle
 - Ground → Geodetic → Grid Distances
- **UNIVERSAL TRANSVERSE MERCATOR COORDINATES (UTM):**
 - US National Grid (USNG)

3. CARTESIAN COORDINATES

- **NORTHING:** $N (Y)$
- **EASTING:** $E (X)$
- **Orthometric Height:** H
(elevation)

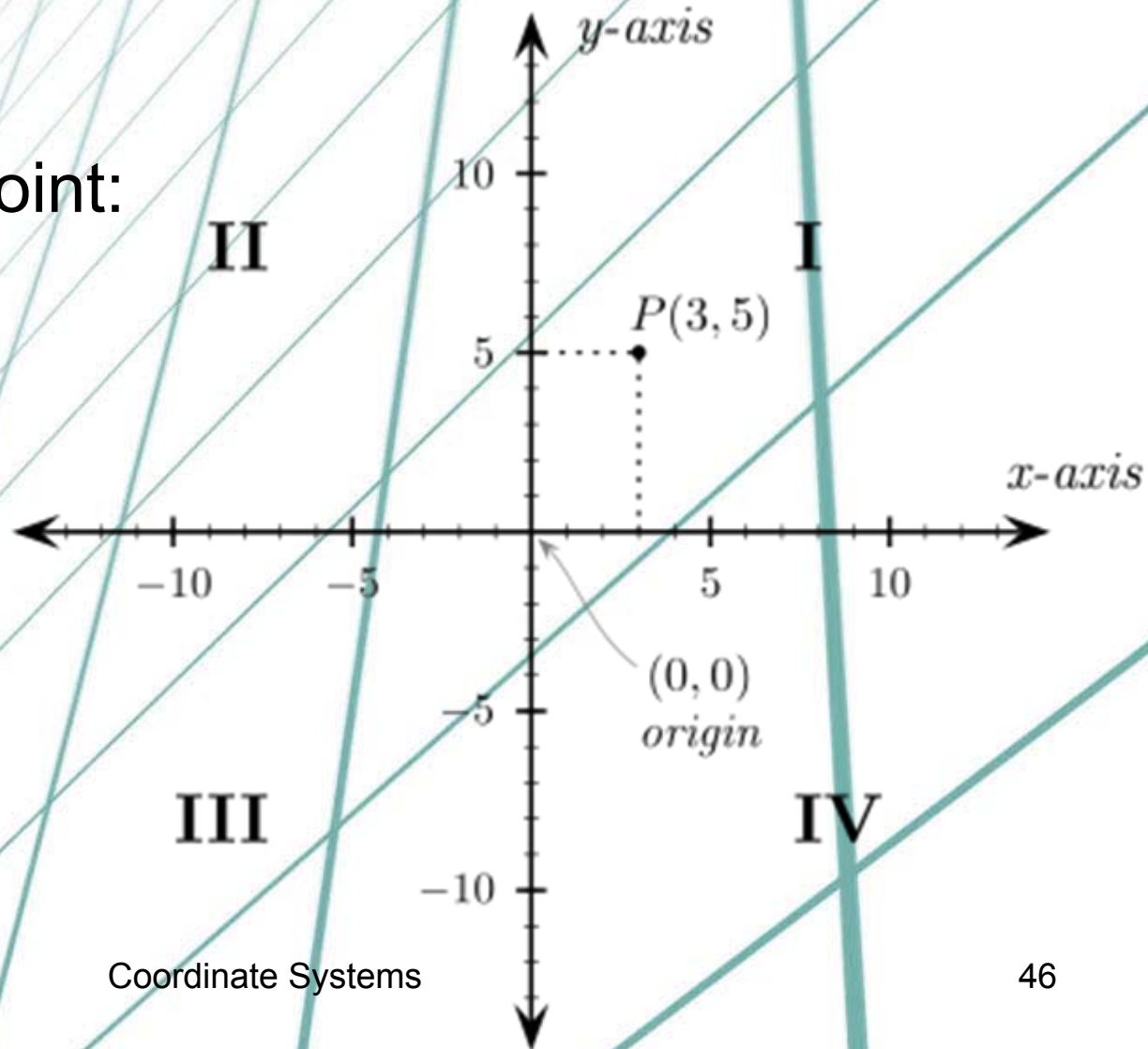
3. CARTESIAN COORDINATES

Two dimensional
coordinates of a point:

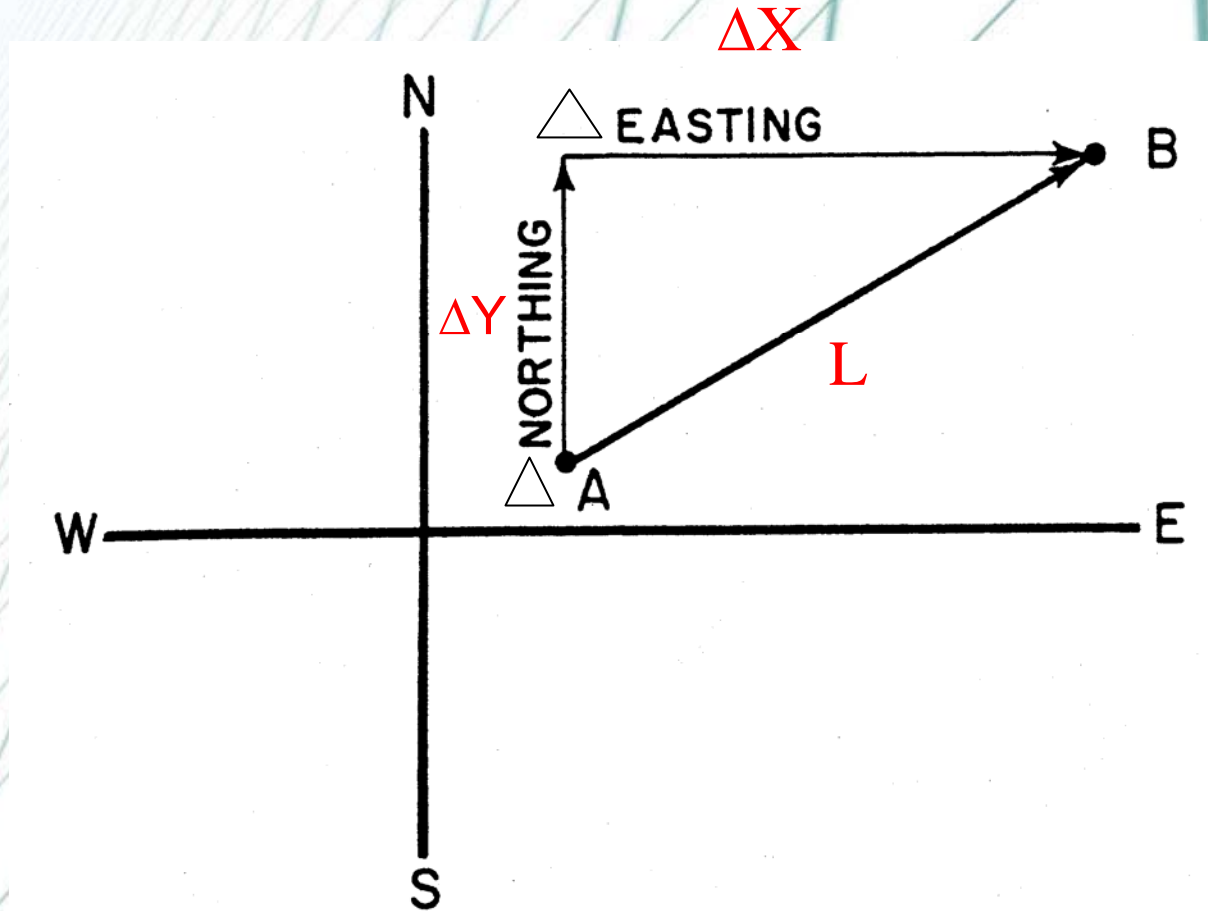
X,Y

or

N,E (Y,X)



3. CARTESIAN COORDINATES



3. CARTESIAN COORDINATES

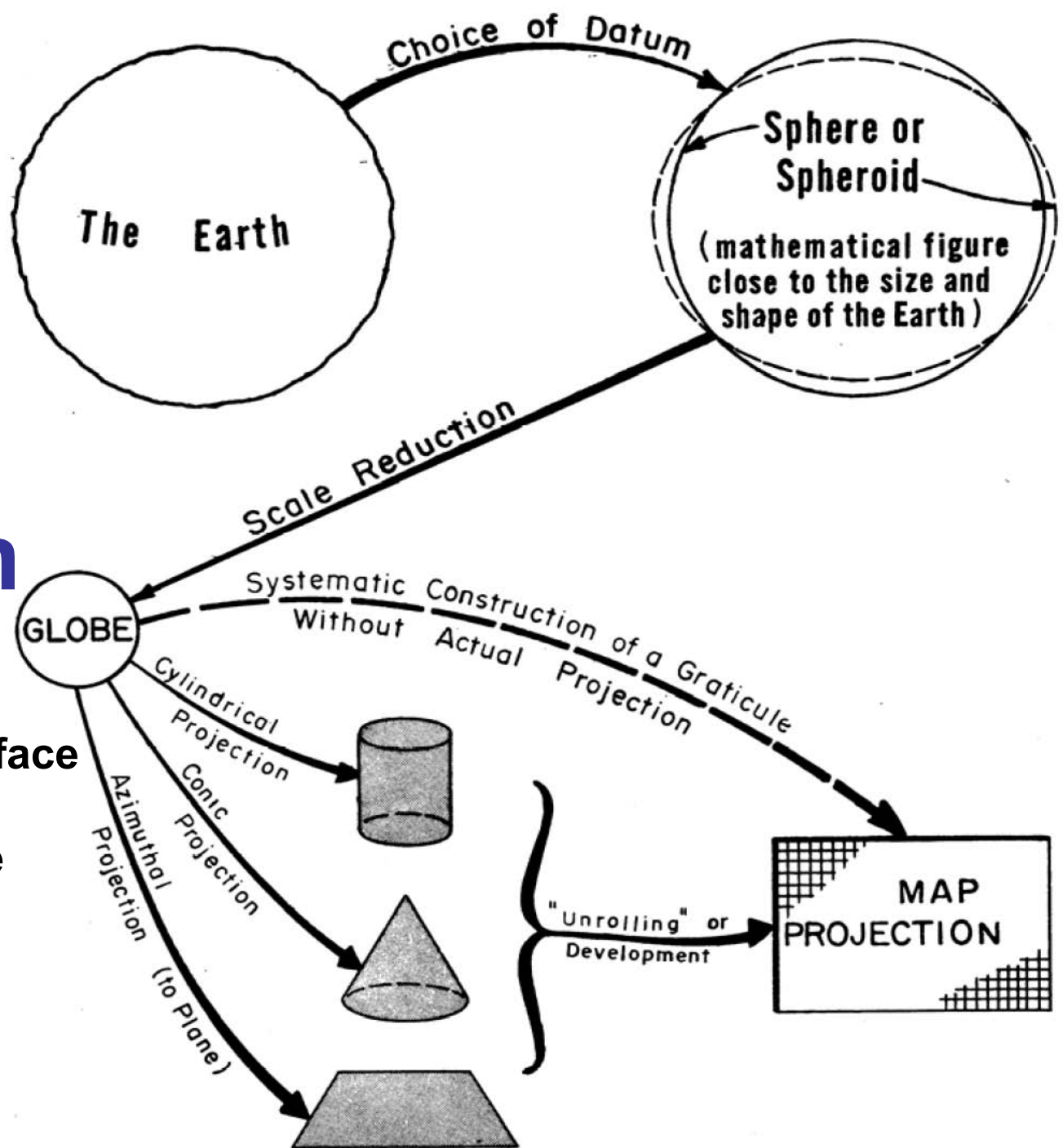
To obtain Cartesian (plane) coordinates from a round surface.

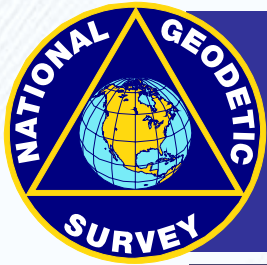
We must “Flatten” the earth by

MAP PROJECTION

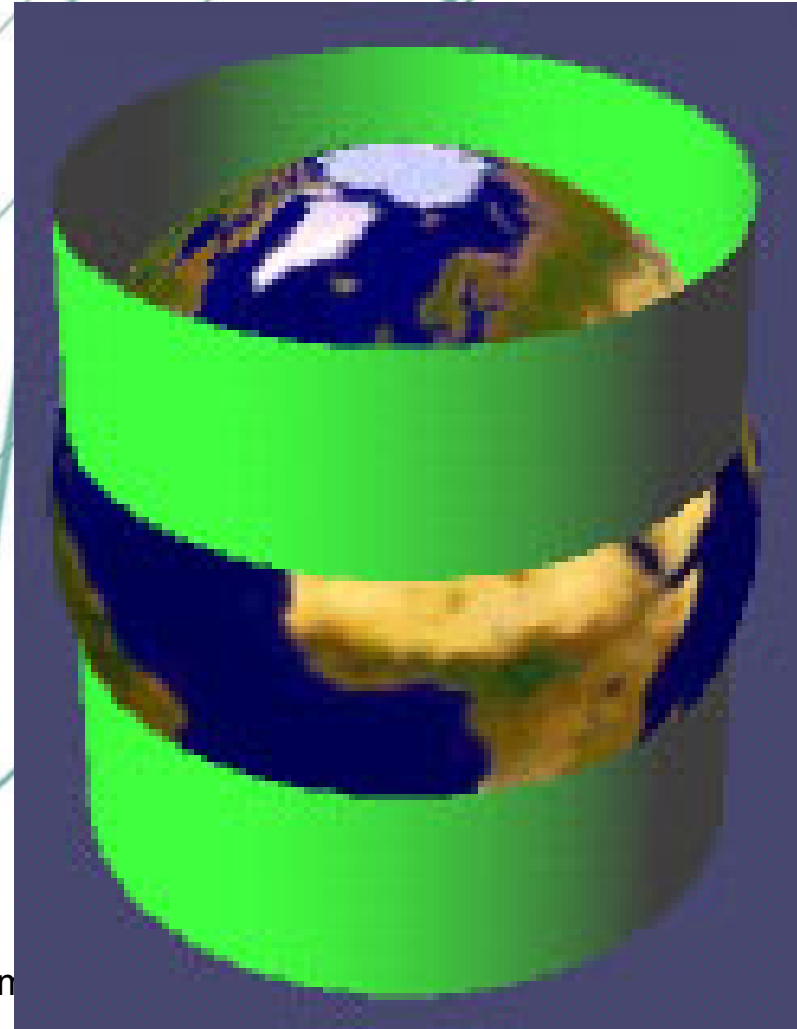
The four steps in Map Projection

- 1 A Mathematical Surface
- 2 Reduce the Scale
- 3 Project on a surface
- 4 Unroll the surface





MAP PROJECTIONS: CONIC AND CYLINDRICAL

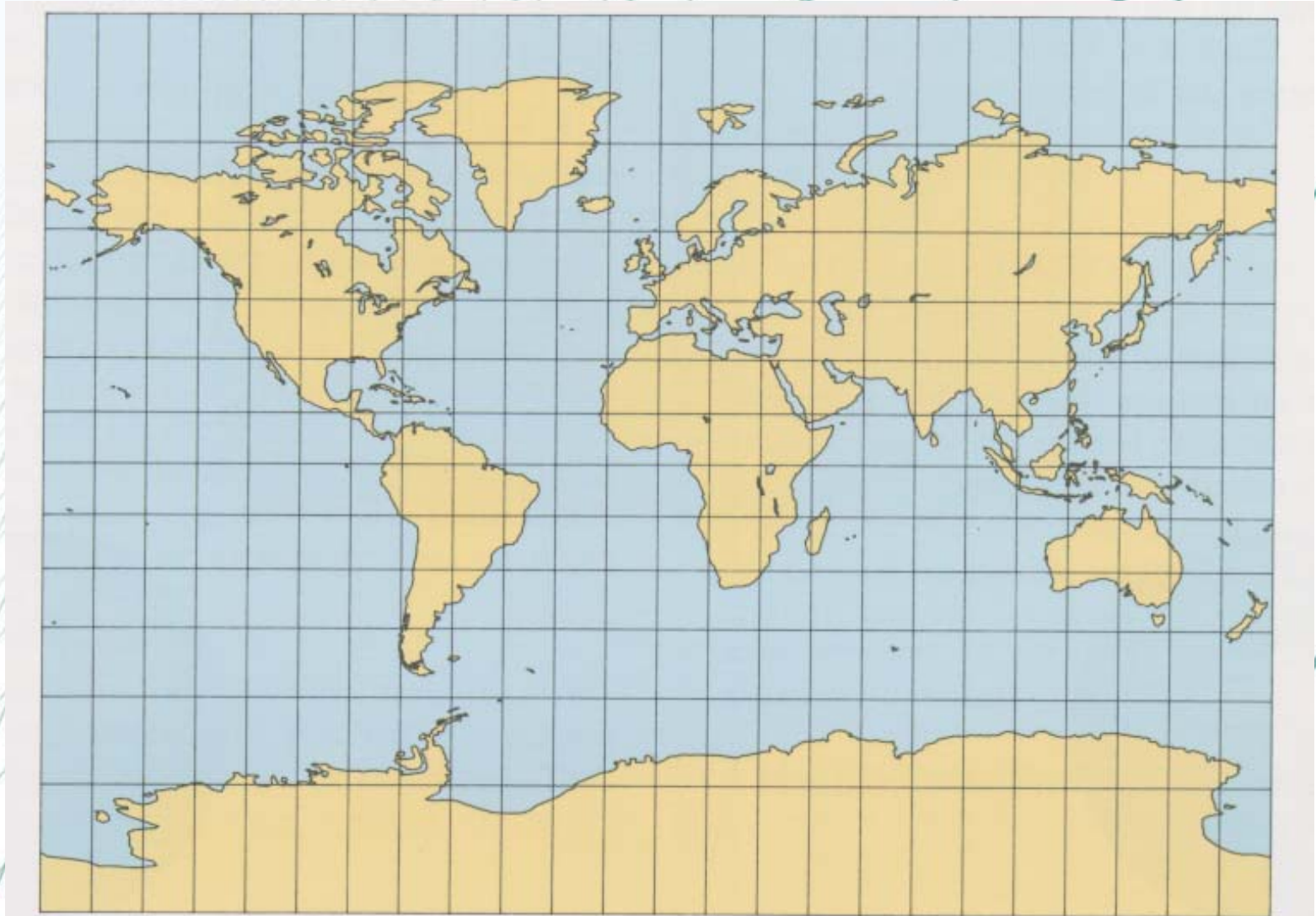


e System

Globe



Flat Map Projection (Mercator)



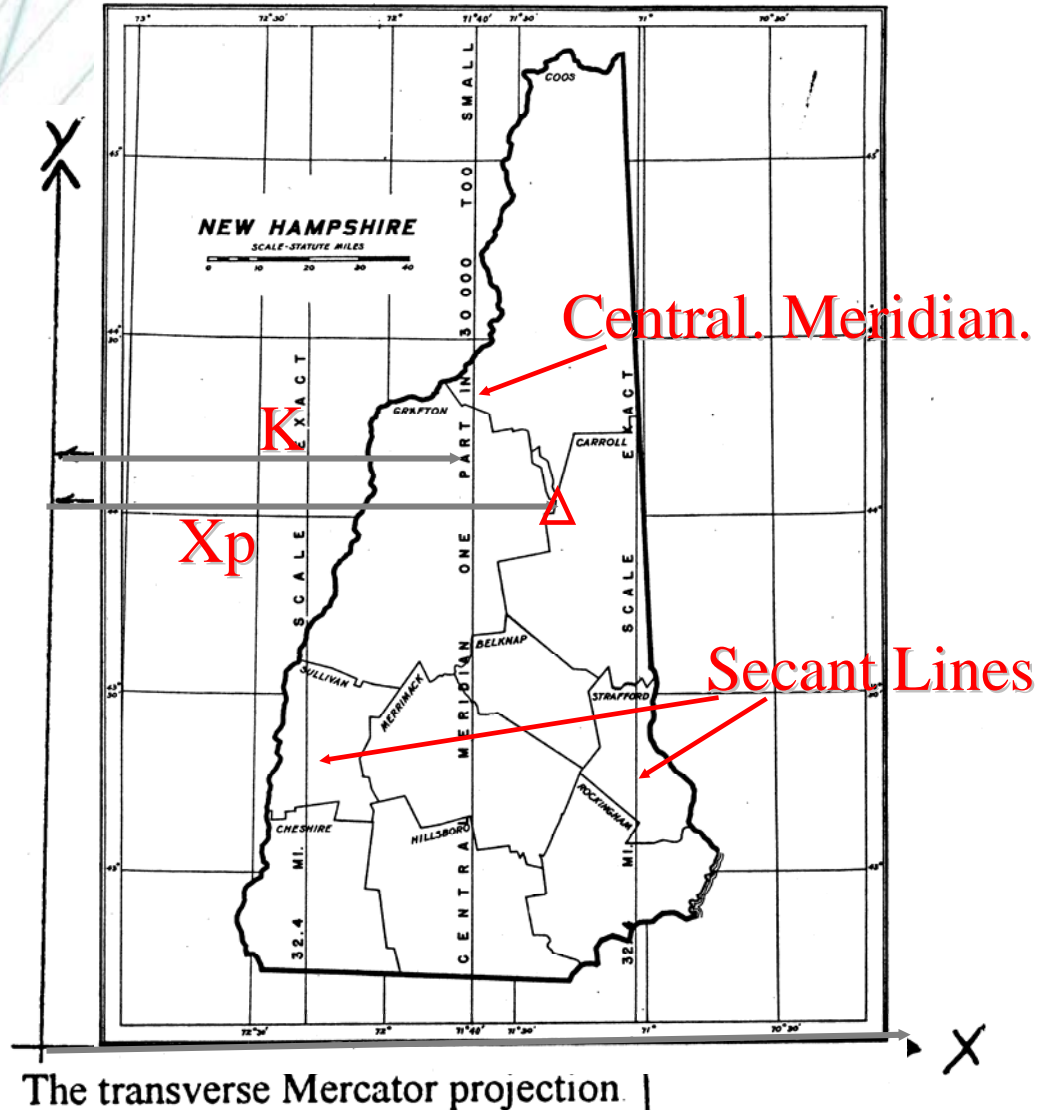
3a. The Transverse Mercator Projection System

New Hampshire State
Plane Coordinates
Based on the
T M System:

Offset of the Central Meridian:

NAD27 System $K = 500,000$ ft.

NAD83 System $K = 300,000$ m



3a. The N.H. State Plane Coordinate System

CENTRAL MERIDIAN IN N.H.

$$\lambda = 71^{\circ} 40'$$

BETWEEN SECANT LINES:

Scale Factor less than 1

OUTSIDE SECANT LINES:

Scale Factor greater than 1

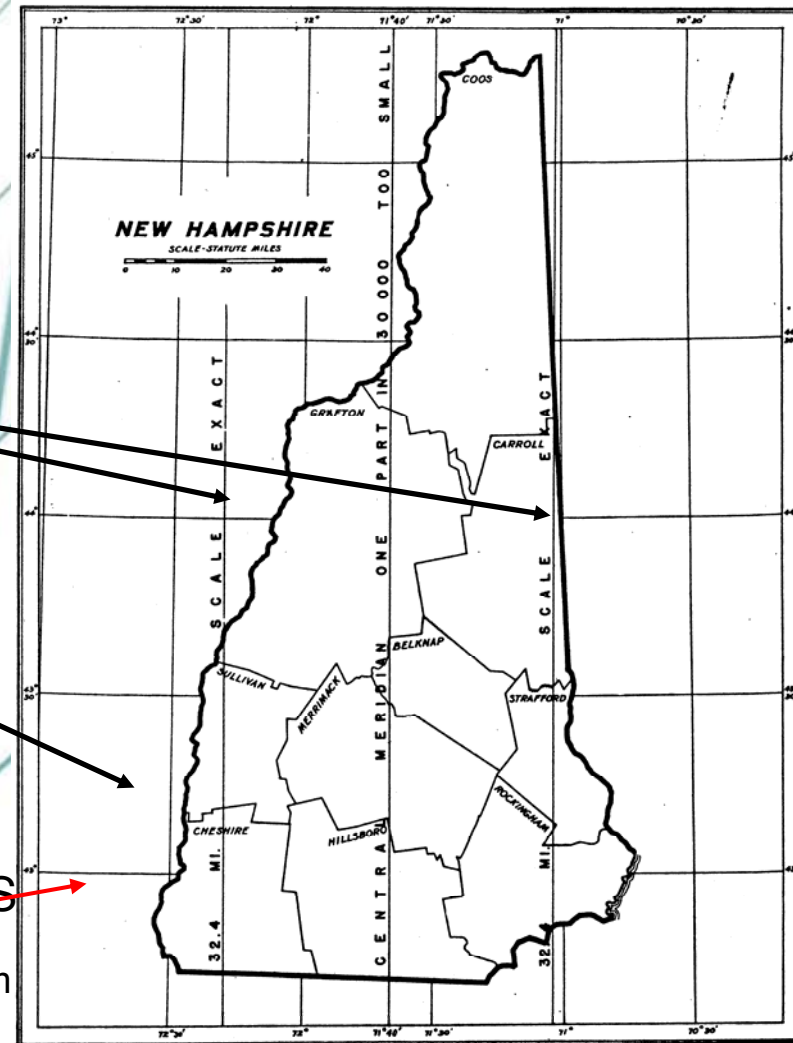
Scale factor constant in N - S direction

Scale Factor varies in the E - W direction

ALSO NOTICE: CONVERGENCE OF MERIDIANS

CURVATURE OF PARALLELS

Coordinate System



Cross-section view of projection

GEOID-ELLIPSOID RELATIONSHIP

$$\text{ELLIPSOID HEIGHT} = \text{ORTHOMETRIC HT} + \text{GEOID HT.}$$
$$h = H + N$$

GEOID UNDULATION

ELLIPSOID
MEAN-SEA-SURFACE-(GEOID)
OCEAN

EARTH'S SURFACE
MOUNTAIN

ORTHOMETRIC HEIGHT OF P
(SEE FIG. 27)

GEOID

GEOID UNDULATION
(SEPERATION)
(HEIGHT)

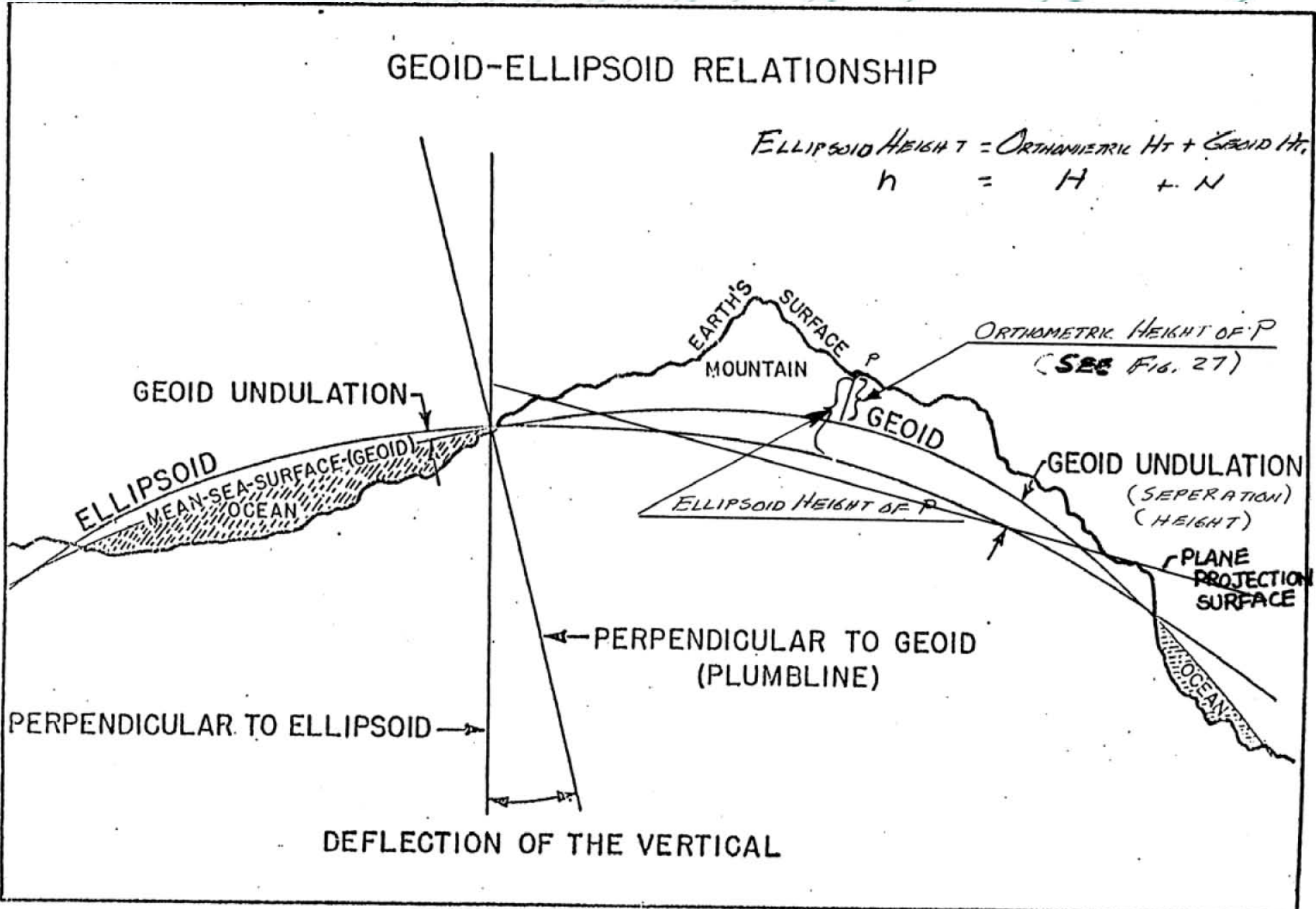
ELLIPSOID HEIGHT OF P

PLANE
PROJECTION
SURFACE

PERPENDICULAR TO GEOID
(PLUMBLINE)

PERPENDICULAR TO ELLIPSOID

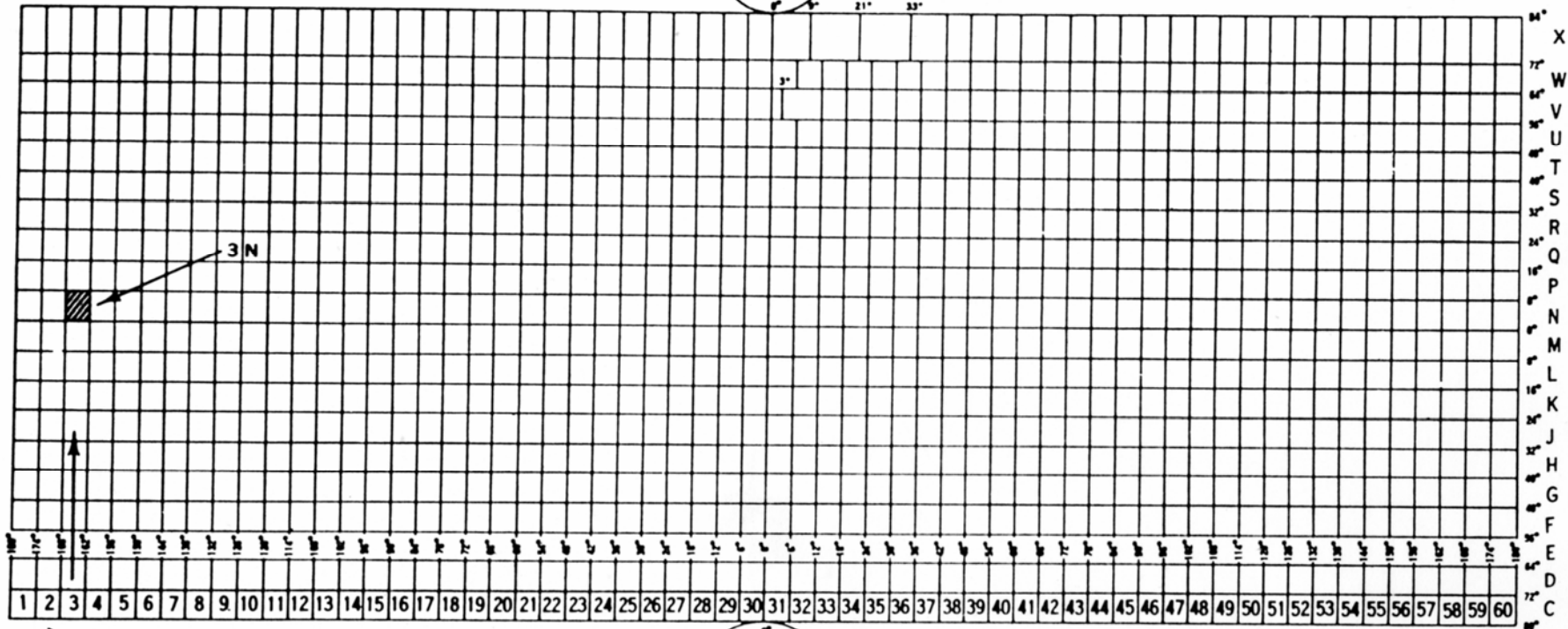
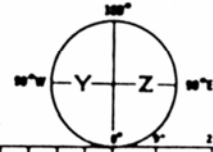
DEFLECTION OF THE VERTICAL



3b. Universal Transverse Mercator Projection System:

80°S to 72° N

6° wide Zones



#'d from 1 to 60

starting at 180°λ

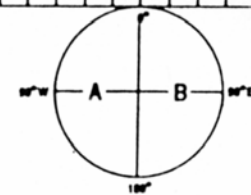


FIGURE 11. – Universal Transverse Mercator (UTM) grid zone designations for the world shown on an Equidistant Cylindrical projection index map.

3b. Universal Transverse Mercator Projection System :

(6° Zones)

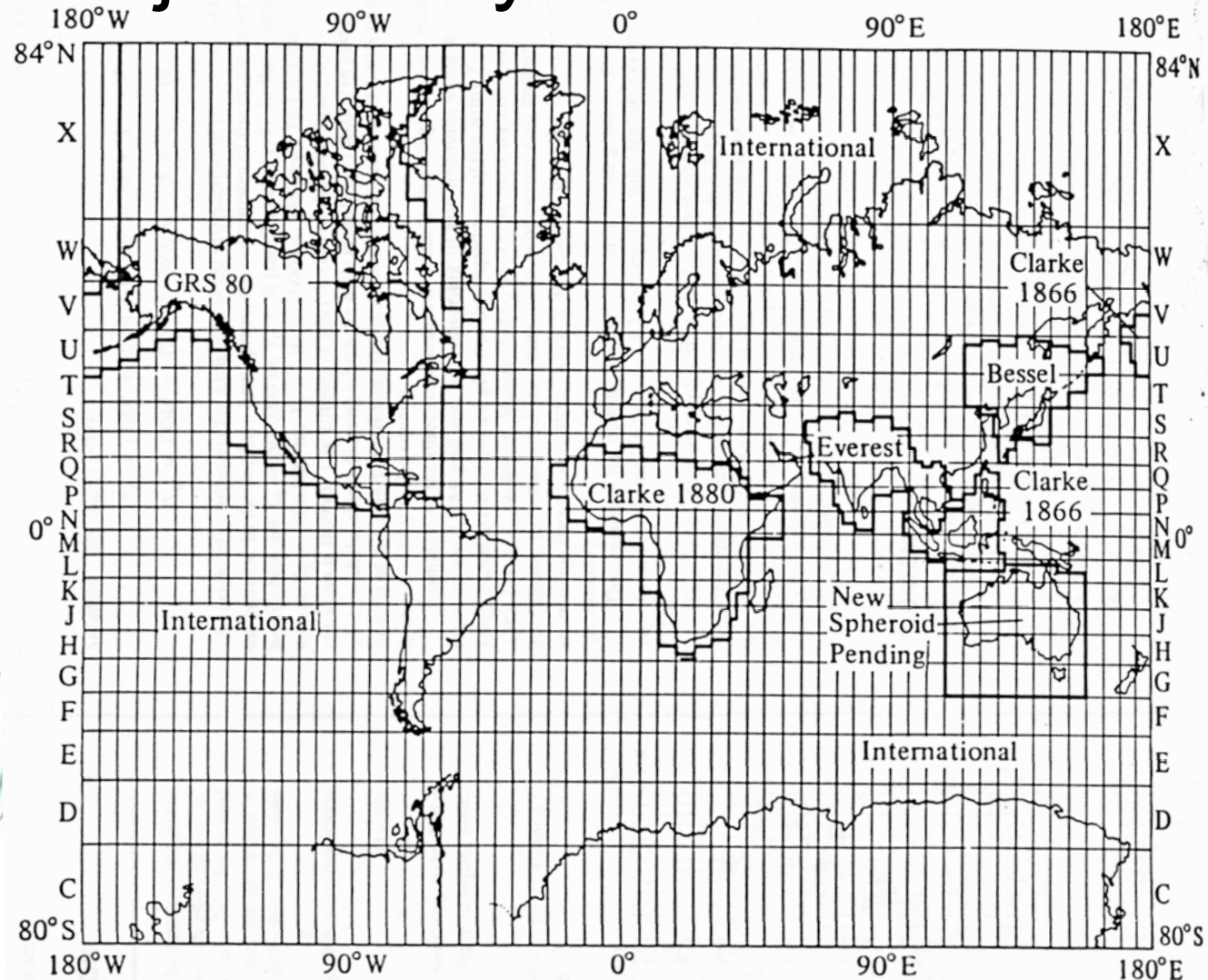
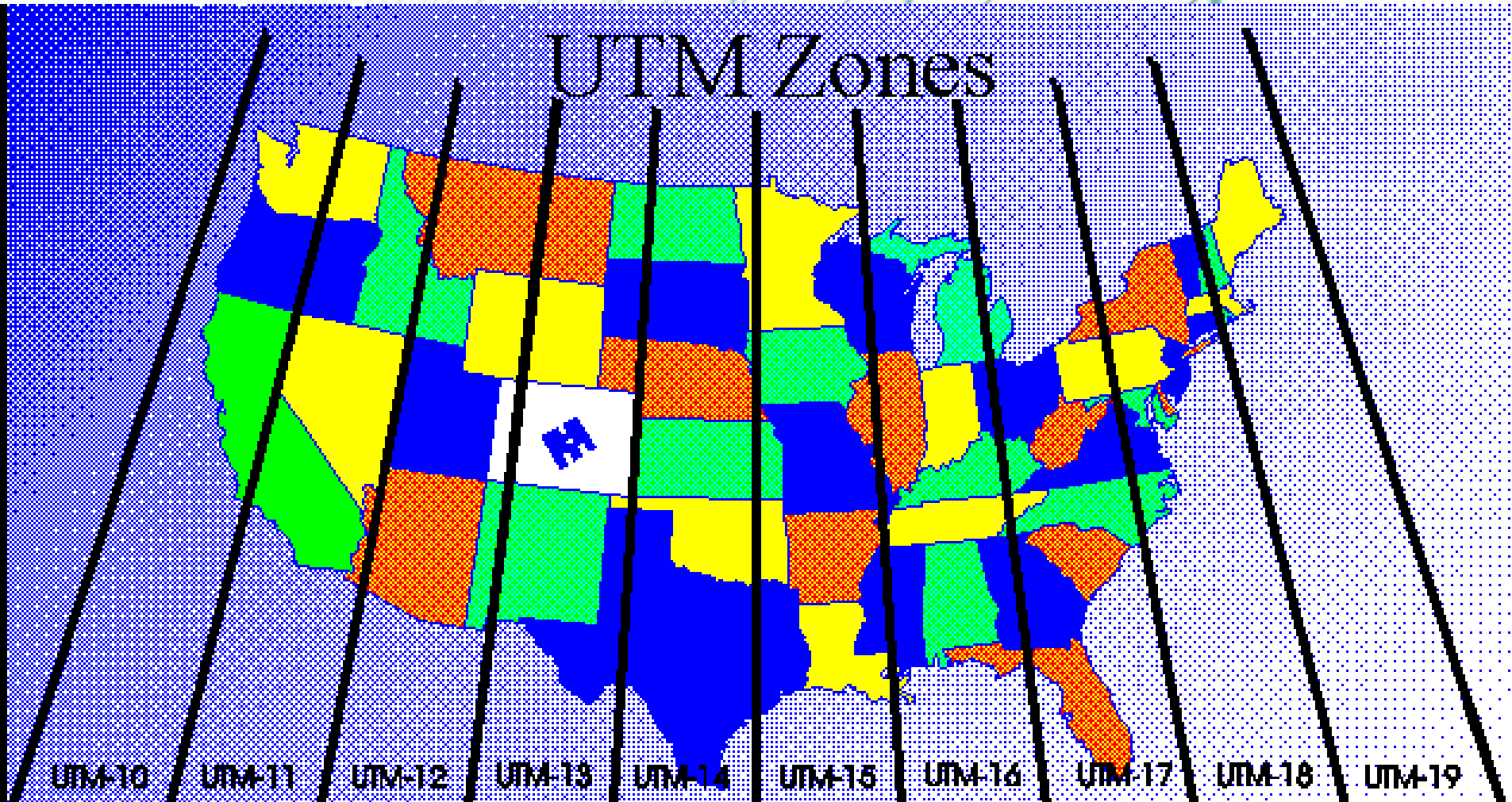


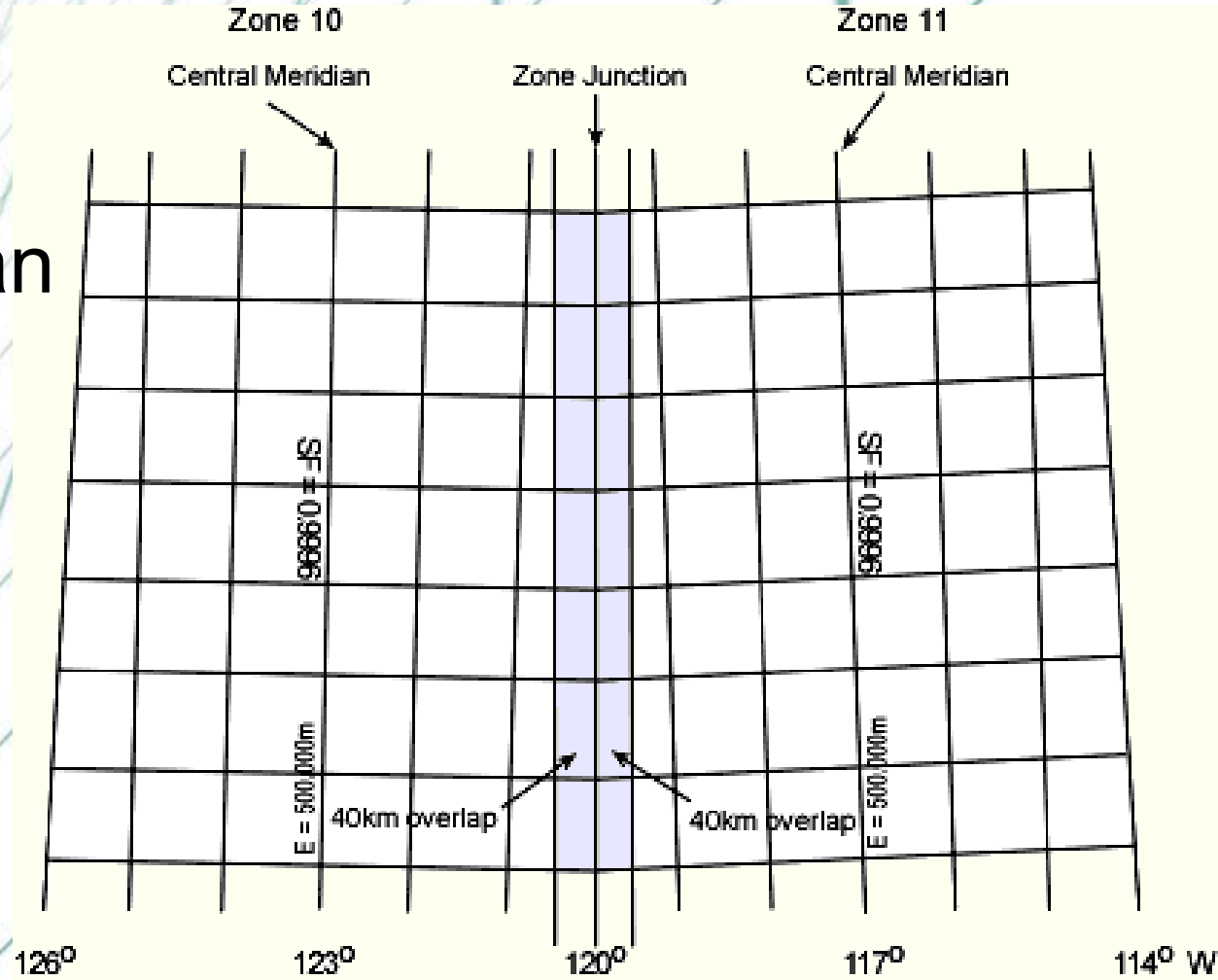
FIGURE 11-14 Universal transverse Mercator (UTM) system. The zones are numbered from 1 to 60 eastward from 180° west longitude.

3b. Universal Transverse Mercator Projection UTM Zones in lower 48 states



3b. Universal Transverse Mercator Projection System (6° Zones) :

Each zone has
a Central Meridian
with
An Easting
of 500,000 m



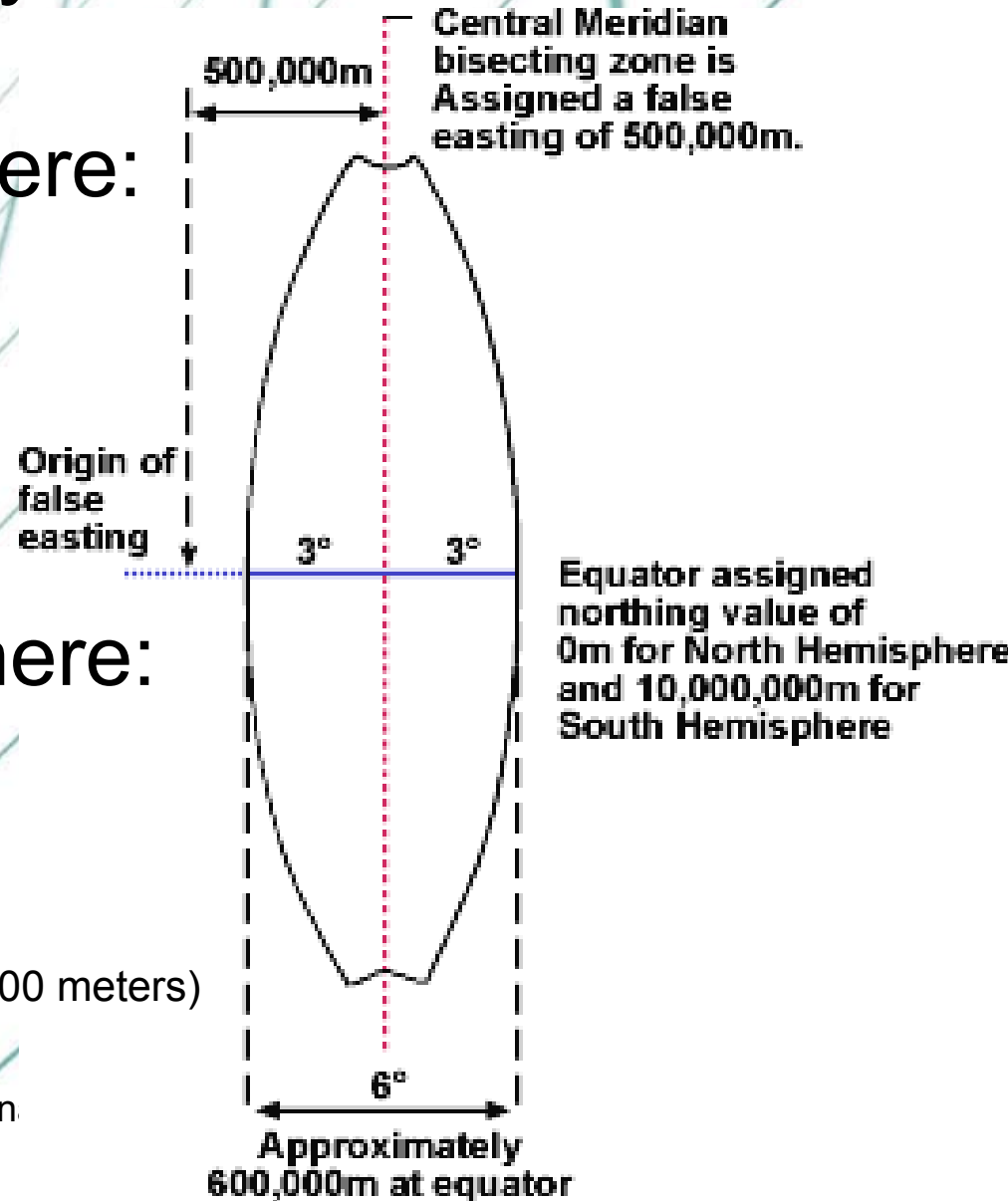
3b. Universal Transverse Mercator Projection System (6° Zones) :

In Northern Hemisphere:
Northing (Y) = 0
At the equator

In Southern Hemisphere:
Northing (Y) = 0
At the South Pole

(equator given a false nothing of 10,000,000 meters)

Coordin



Universal Transverse Mercator Projection

NH in two
different zones,
18 & 19

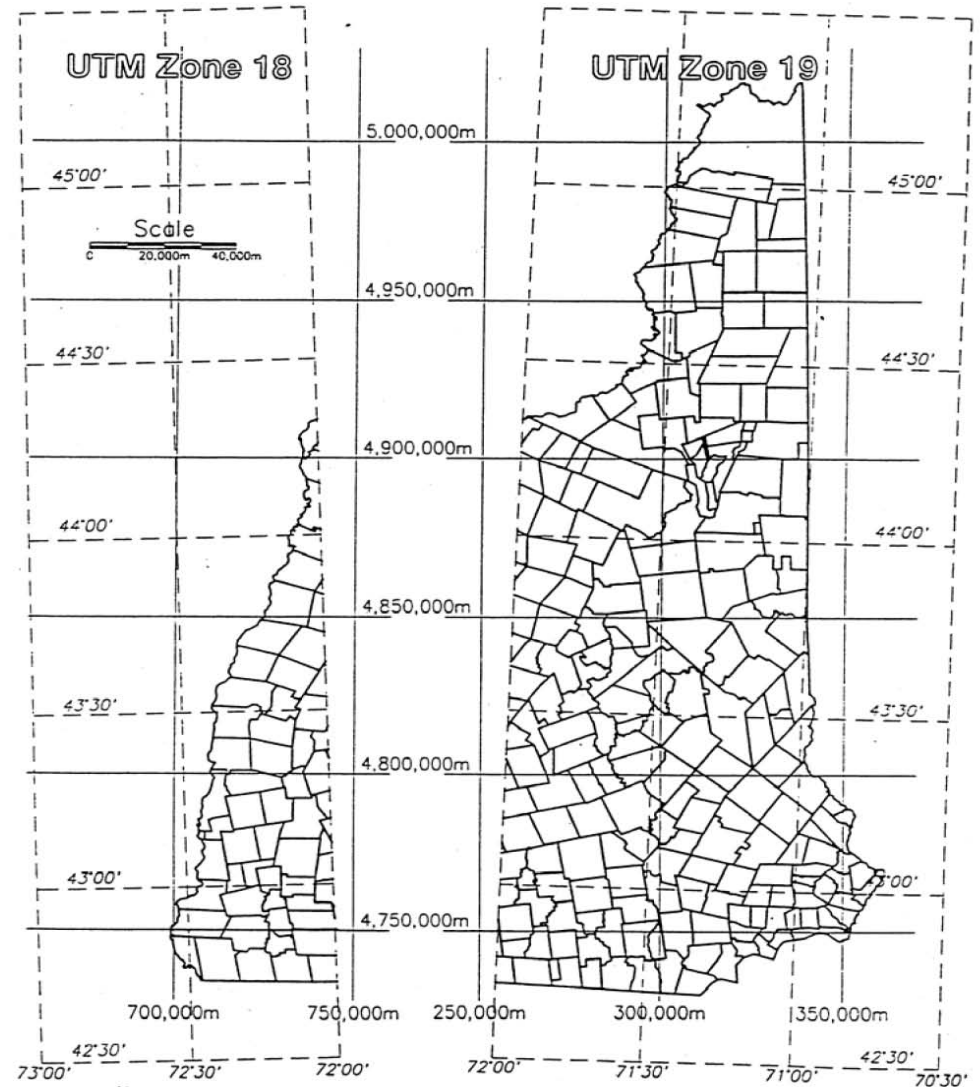


Figure 2.7 - State of New Hampshire (state and town boundaries), in UTM coordinates, Zones 18 and 19. Coordinate grid units are in meters.

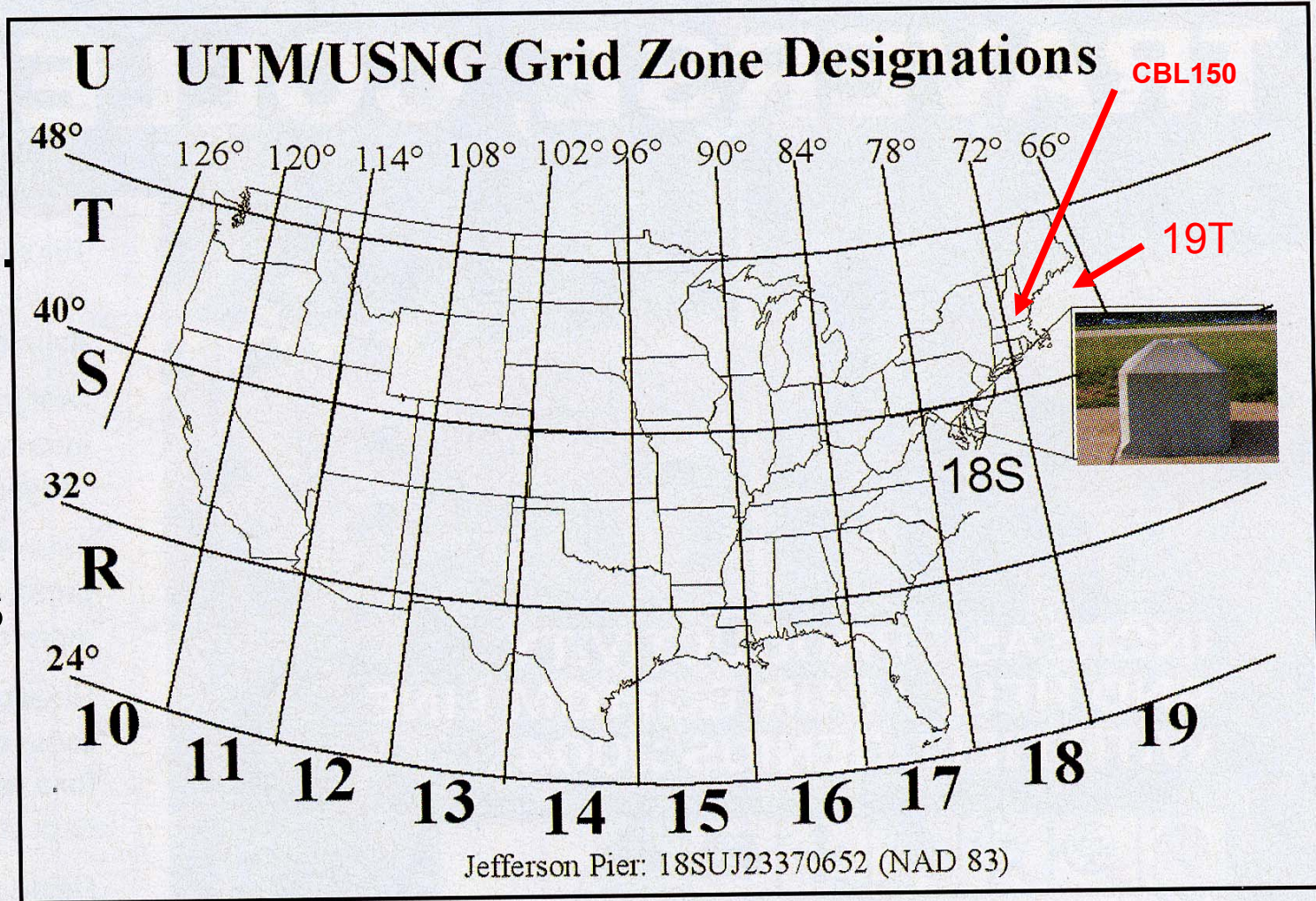
3c. The United States National Grid (USNG)

- An alphanumeric point reference system that overlays the UTM System
- Similar to the US Military Grid Reference System (MGRS)
- Is the FGDC Standard
- Is the Department of Homeland Security recommended system

3c. The United States National Grid (USNG)

GZD's

6° Long.
By
8° Lat.
Quad-
rangles



Prof. Surv. Magazine

Figure 5 USNG Grid Zone Designations over the conterminous United States.

3c. The United States National Grid (USNG)

Each GZD has a scheme of 100KM Squares

The ID Designation Is a pair of letters
AA through ZV
(no letters I or O used)

FGDC-STD-011-2001

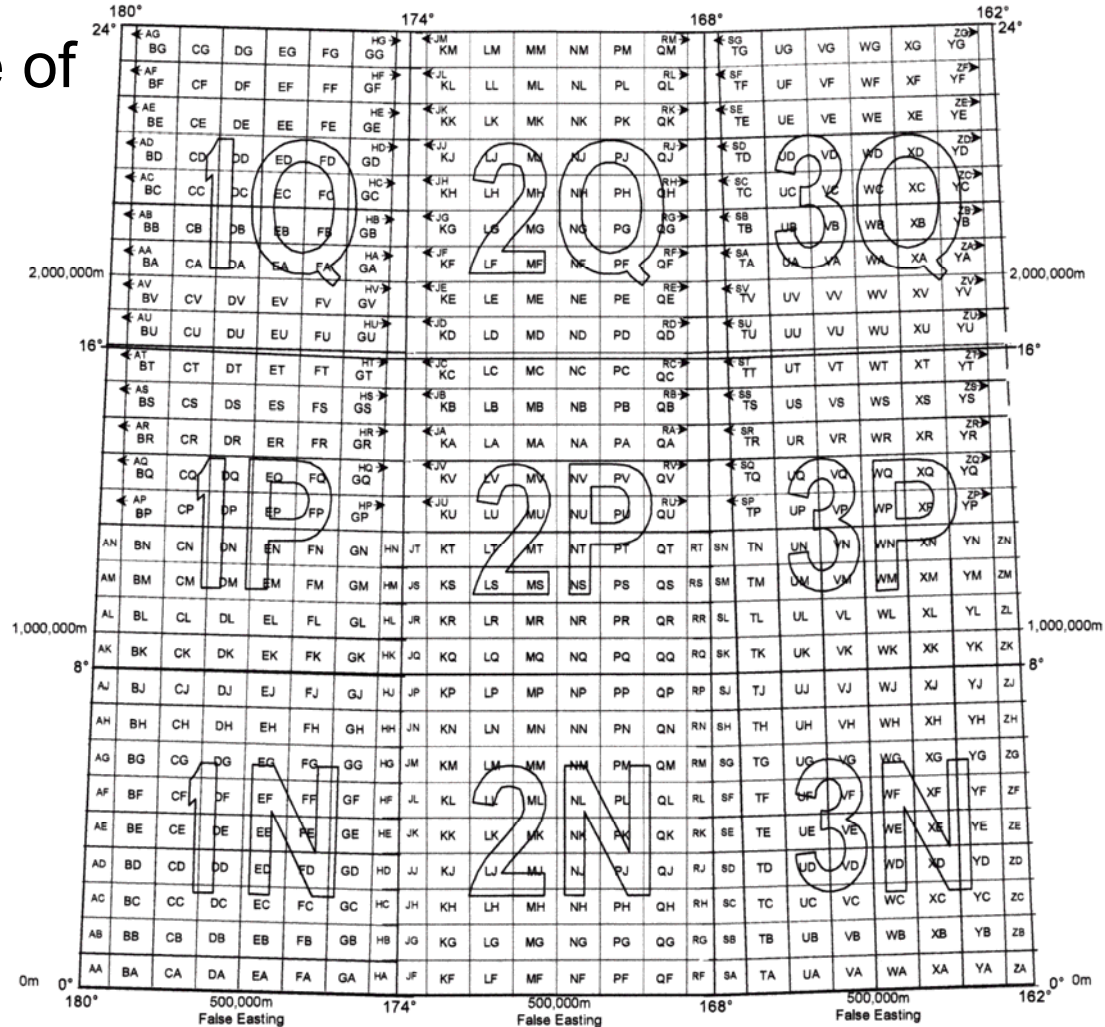
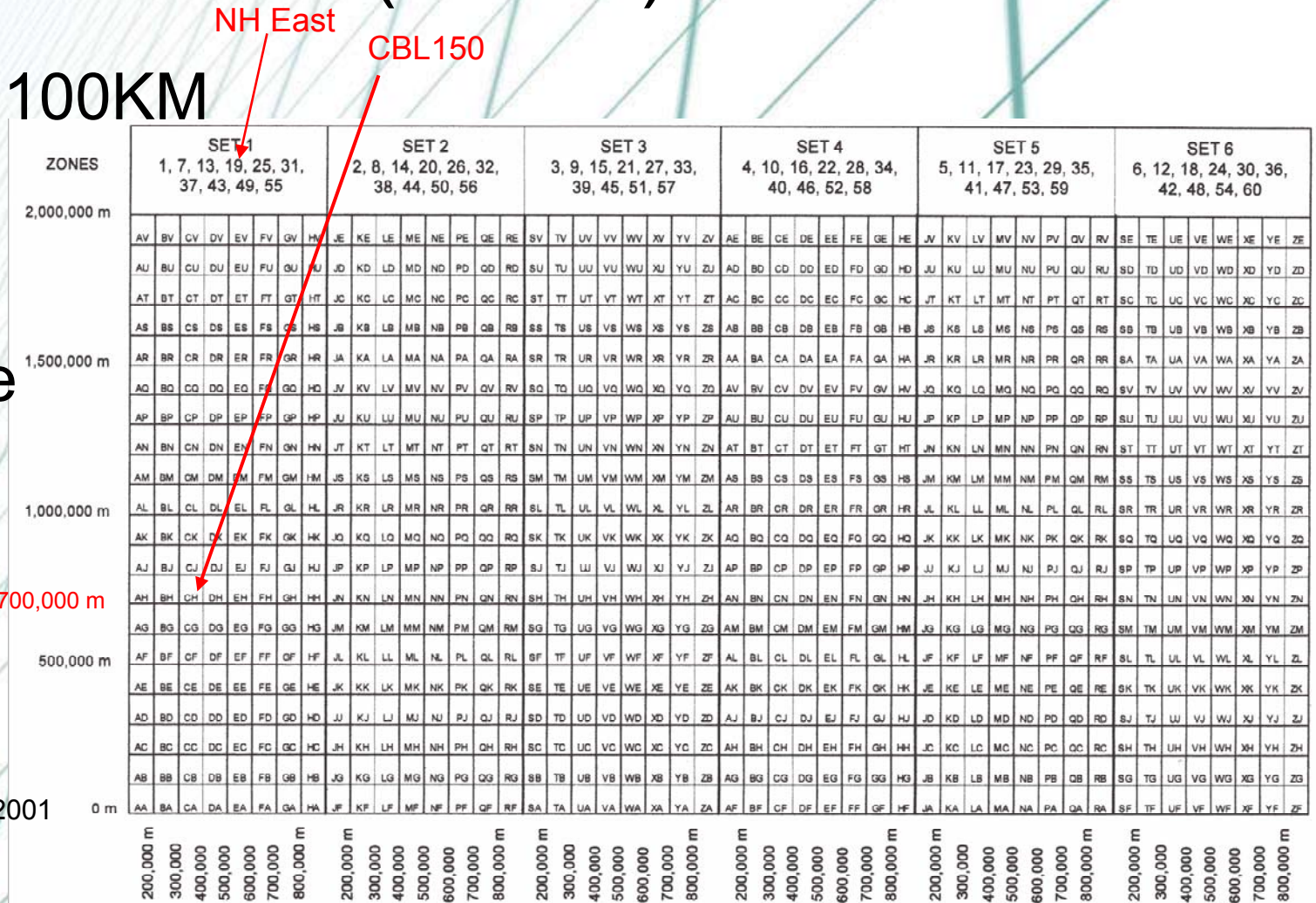


Figure 2. Basic Plan of the 100,000-meter Square Identification of the United States National Grid (USNG)

3c. The United States National Grid (USNG)

Plan of 100KM
 Square
 ID's
 by Zone
 (SET)



FGDC-STD-011-2001

Figure 3. Organization of the U.S. National Grid (USNG) 100,000-meter Grid Squares

3c. The United States National Grid (USNG

Station CBL150:

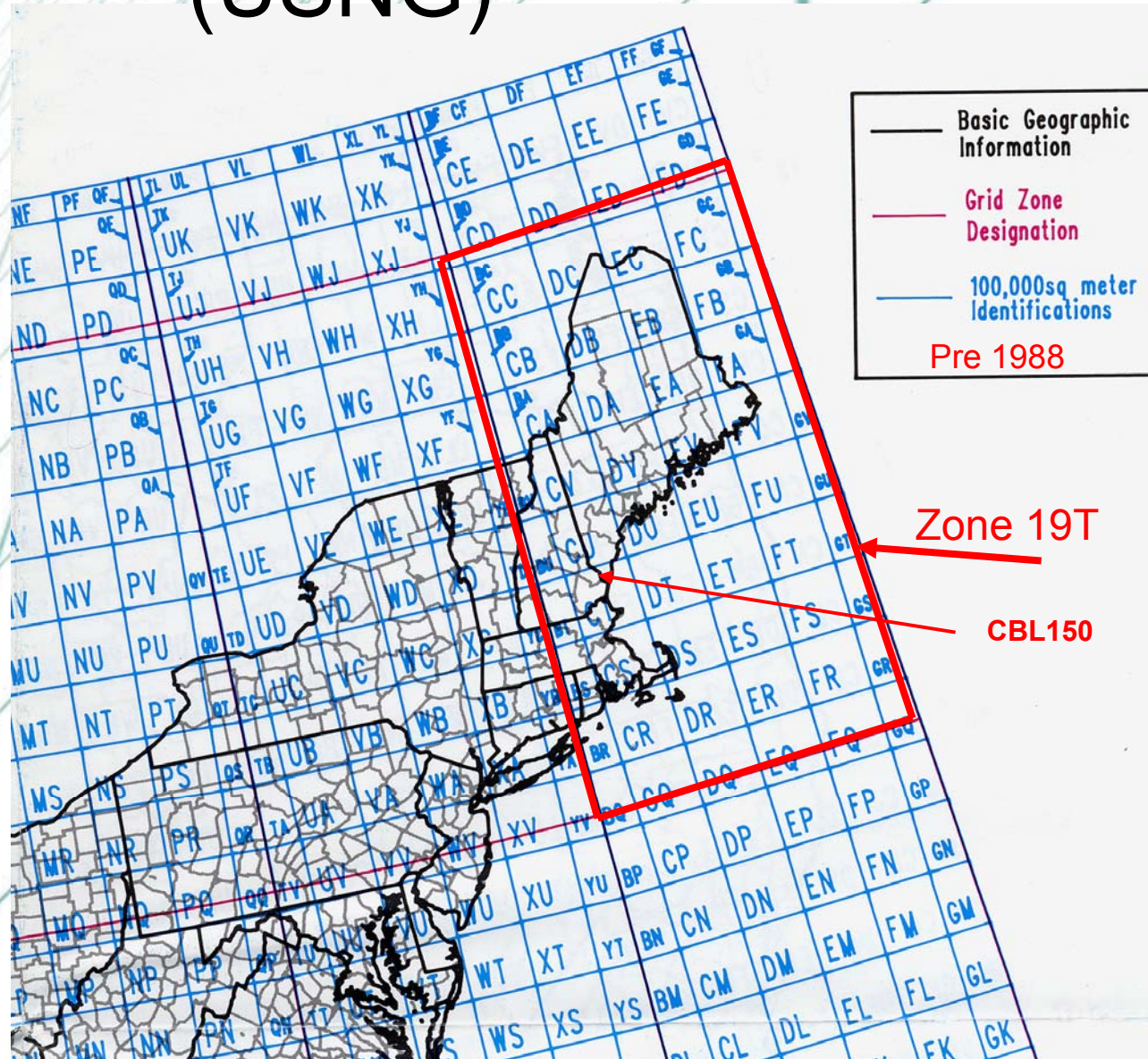
Calibration Base Line 150 (meters)
UNH – Durham, N.H.

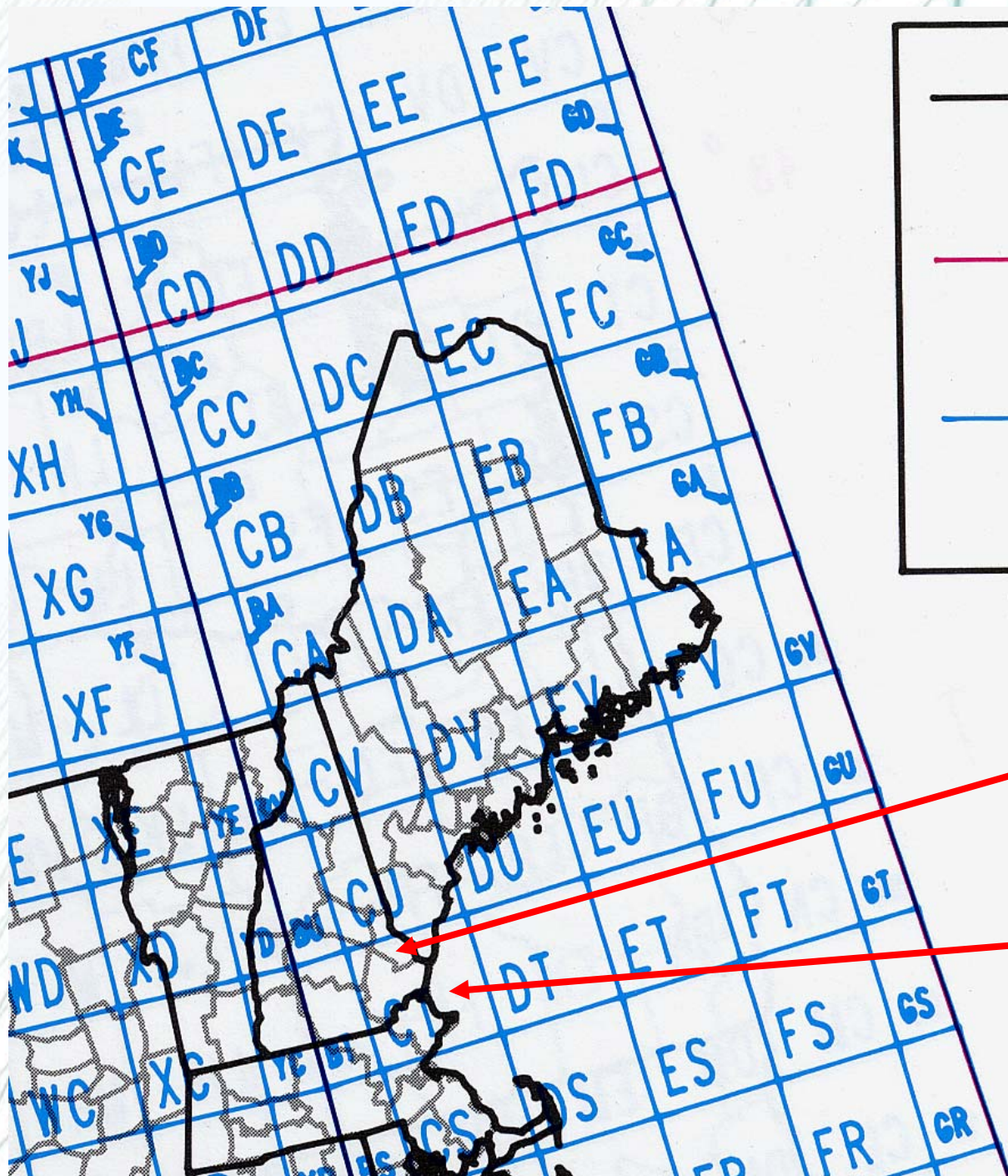


3c. The United States National Grid (USNG)

Example of
100,000 meter
square ID
In NE.

The ID Designation
Is a pair of letters
AA through ZV
(no letters I or O used)





Basic Geographic Information

Grid Zone Designation

100,000sq meter Identifications

Pre 1988

CBL 150

100KM Square ID
"CH" in NG

3c. The United States National Grid (USNG)

So a USGN Geoaddress consists of:

1- **Grid Zone Designation (GZD):**

two digits and one letter (19T)

(C to X, no letter I or O used)

2- **100 km Square ID:**

a pair of letters (AA –ZV) (19T CH)

(no letters I or O used)

3- **Grid Coordinates:**

Easting, Northing (X,Y) in Meters

3c. The United States National Grid (USNG)_(100 KM Squares) :

Station CBL150:

Calibration **Base Line 150** (meters)

UTM Coordinates:

E = 342,180.681 m

N = 4,778,260.946 m

So

USNG Position:

19TCH4218078260NAD83

If 5 coordinate digits, then to nearest meter

If 4 coordinate digits, then to nearest 10 meters



3c. The United States National Grid (USNG)

So a USGN Geoaddress consists of:

1- **Grid Zone Designation (GZD):**

two digits and one letter (19T)

(C to X, no letter I or O used)

2- **100 km Square ID:**

a pair of letters (AA –ZV) (19T CH)

(no letters I or O used)

3- **Grid Coordinates:**

Easting, Northing (X,Y) in Meters

(19TCH4218078260)

3c. The United States National Grid (USNG)

Another Example:

A point with coordinates:

682,725 M East 5,091,275 M North UTM Zone 19 NAD83

Would be designated as”

19TFL8272591275NAD83

19T Grid Zone Quadrangle ($6^\circ \lambda$ by $8^\circ \Phi$ Quadrangle)

FL 100 KM Square

82725 Truncated Easting

91275 Truncated Northing

NAD83 The Horizontal Datum used in the projection

3c. The United States National Grid (USNG) (100 KM Squares) :

A third
example:

The
Jefferson Pier:
Planned to be the
First Meridian
Of the US

18S UJ 2337 0652

Prof. Surv. Magazine

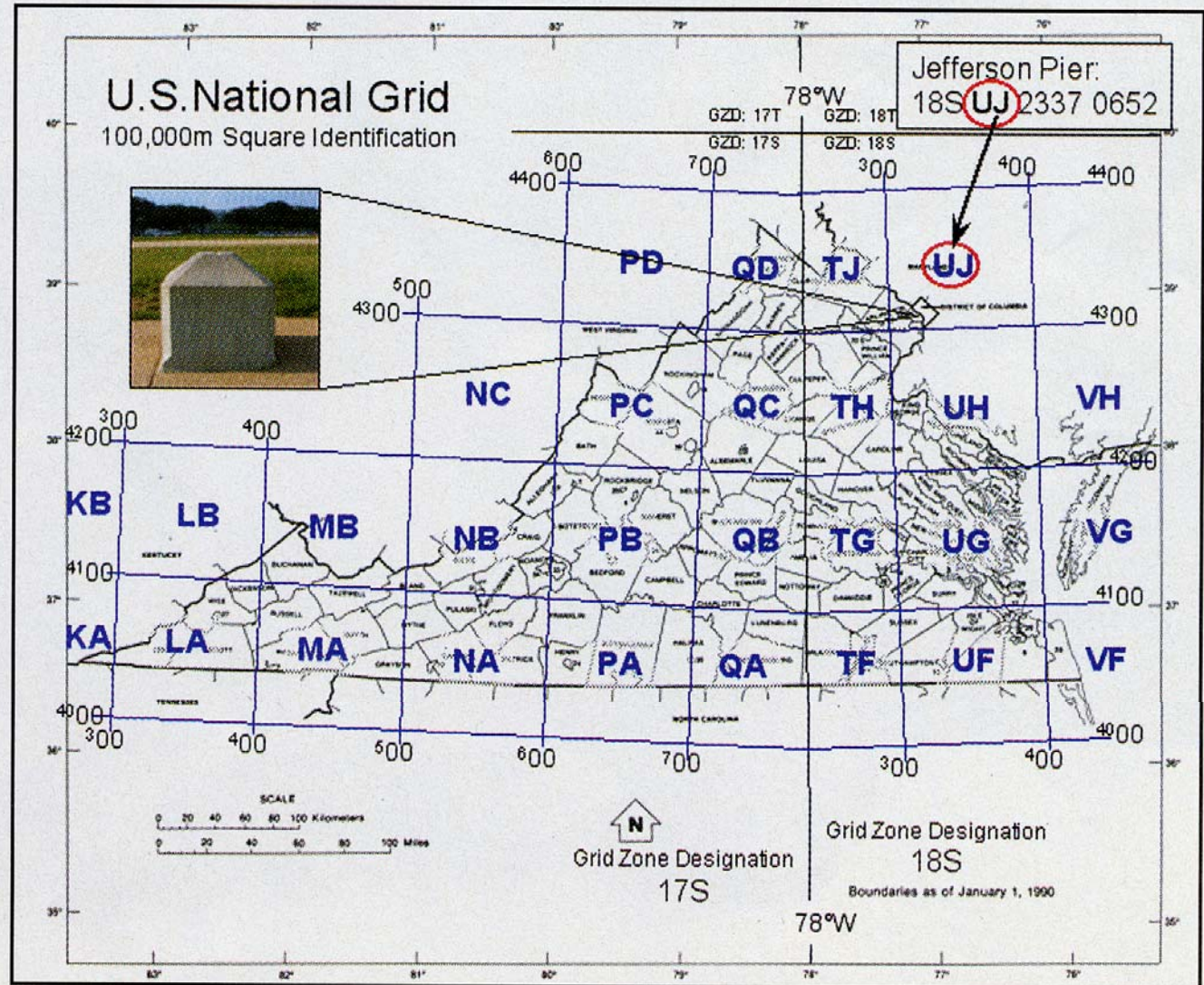


Figure 3 The USNG 100,000-meter Square Identification scheme over Virginia

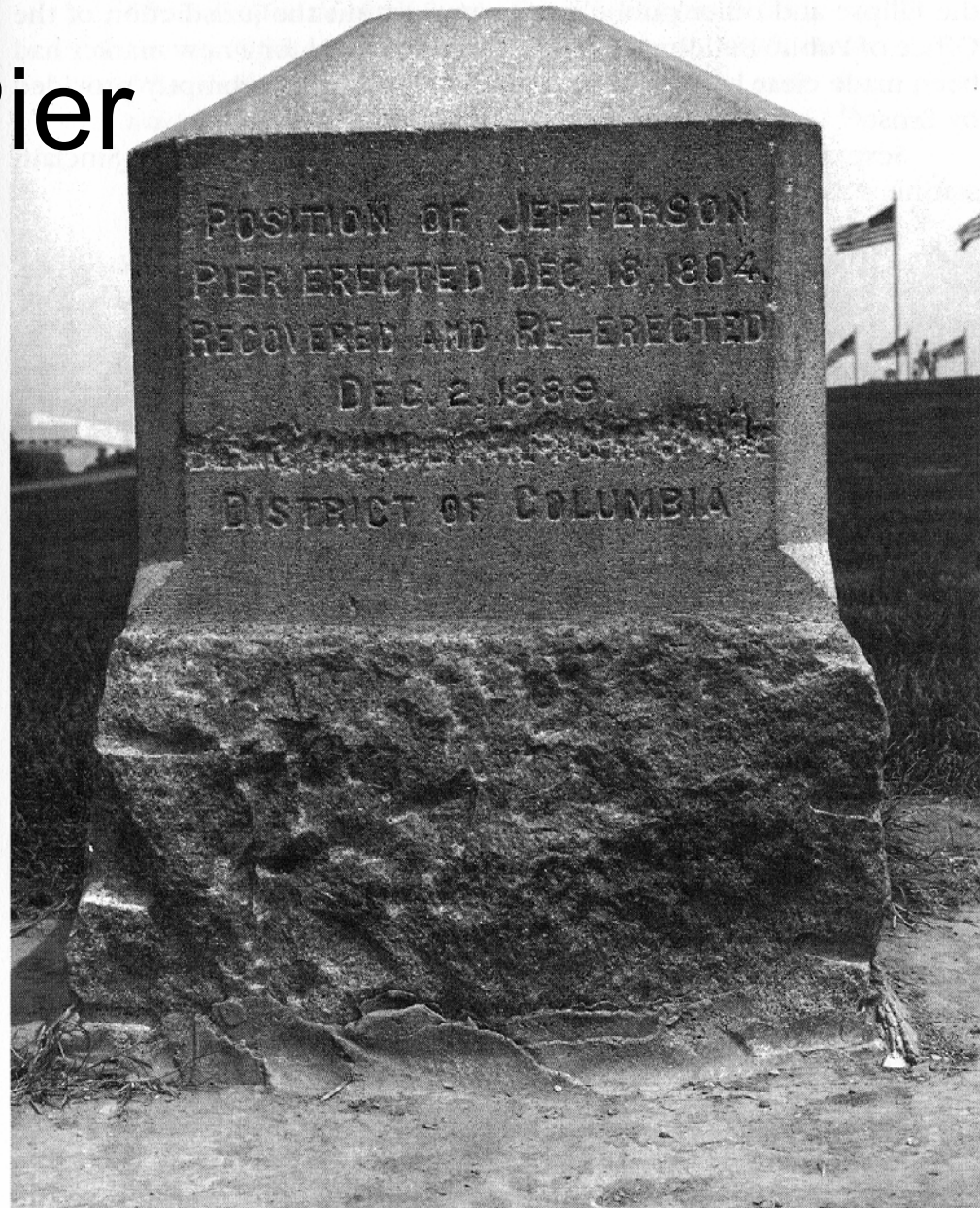
The Jefferson Pier

Read

"The Jefferson Stone"

1999

By Silvio A. Bedini



Coc

Figure 38. The west face of the Jefferson Pier Monument as it appeared in 1975. Since then the area surrounding it has been regraded to raise the soil level.

The Jefferson Pier

*“The
Jefferson
Stone”*
1999
Silvio A.
Bedini



Figure 43. The Jefferson Pier Monument. Photograph by Leandra A. Bedini.

3c. The United States National Grid (USNG) (100 KM Squares) :

The Jefferson Pier

18S UJ 2337 0652

Prof. Surv. Magazine

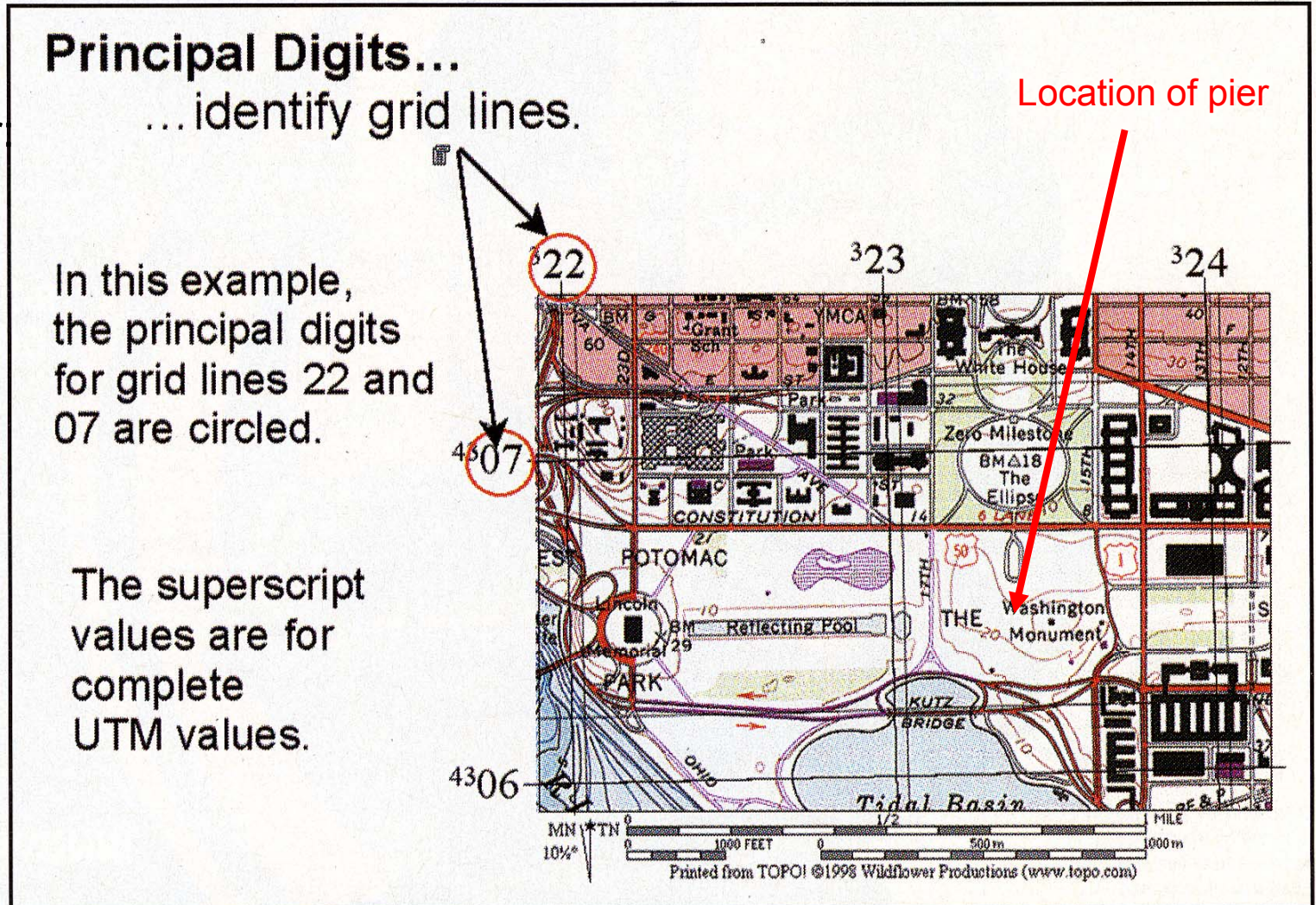


Figure 1 Principal Digits identify grid lines

The background features a series of teal-colored lines that converge towards the left side of the frame, creating a sense of depth and perspective. The lines vary in thickness and are set against a light, almost white background.

THREE DISTANCES

THREE DISTANCES

1. GROUND DISTANCE

Slope distance between two points

2. ELLIPSOID (GEODETIC) DISTANCE

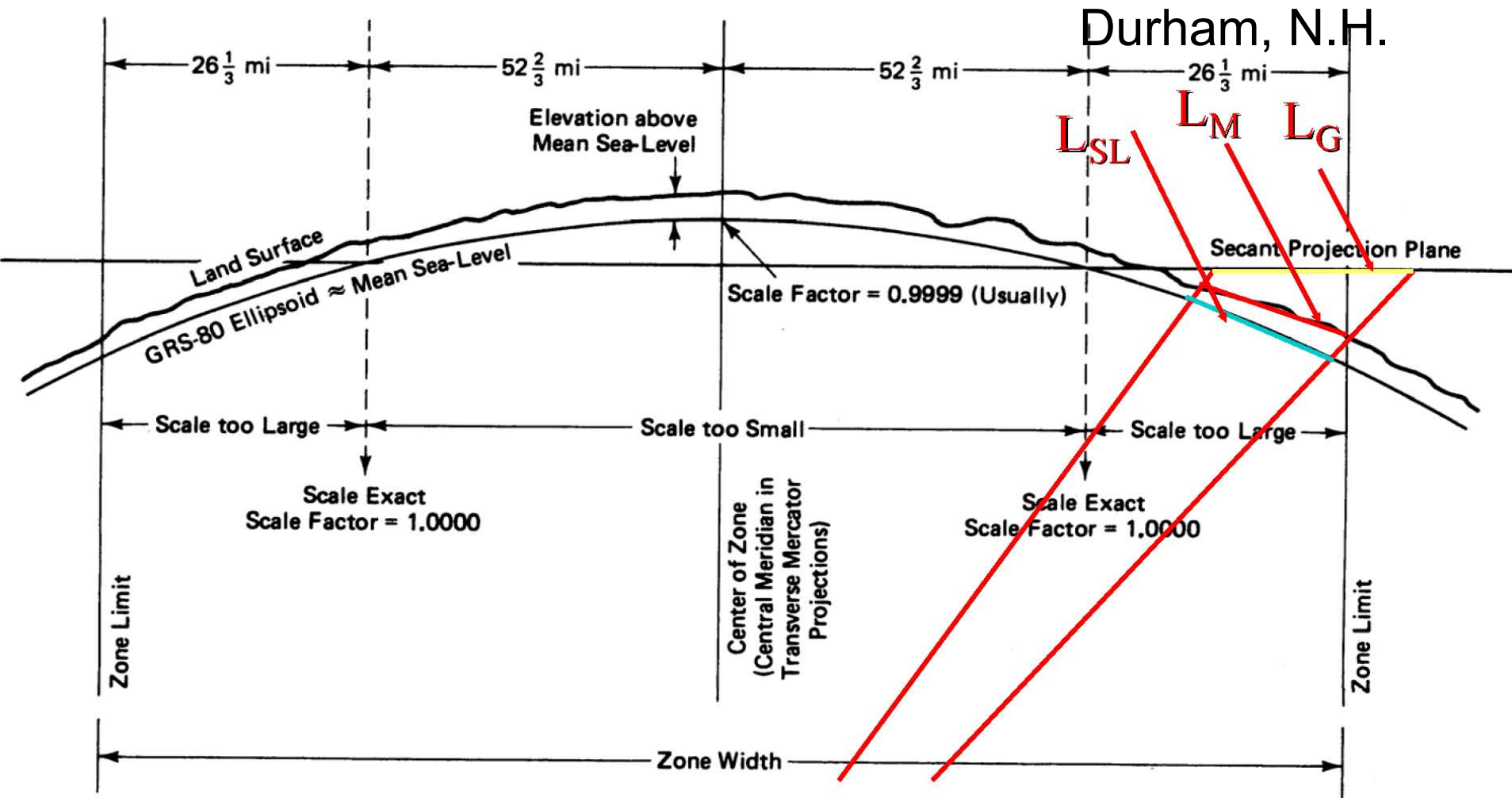
Curved distance on Ellipsoid between two points

3. GRID DISTANCE

Horizontal distance on Plane between two points

Ground – Ellipsoid - Grid Distances

L_{SL} = Sea Level (Geodetic) Dist. L_M = Ground Dist. L_G = Grid Dist.



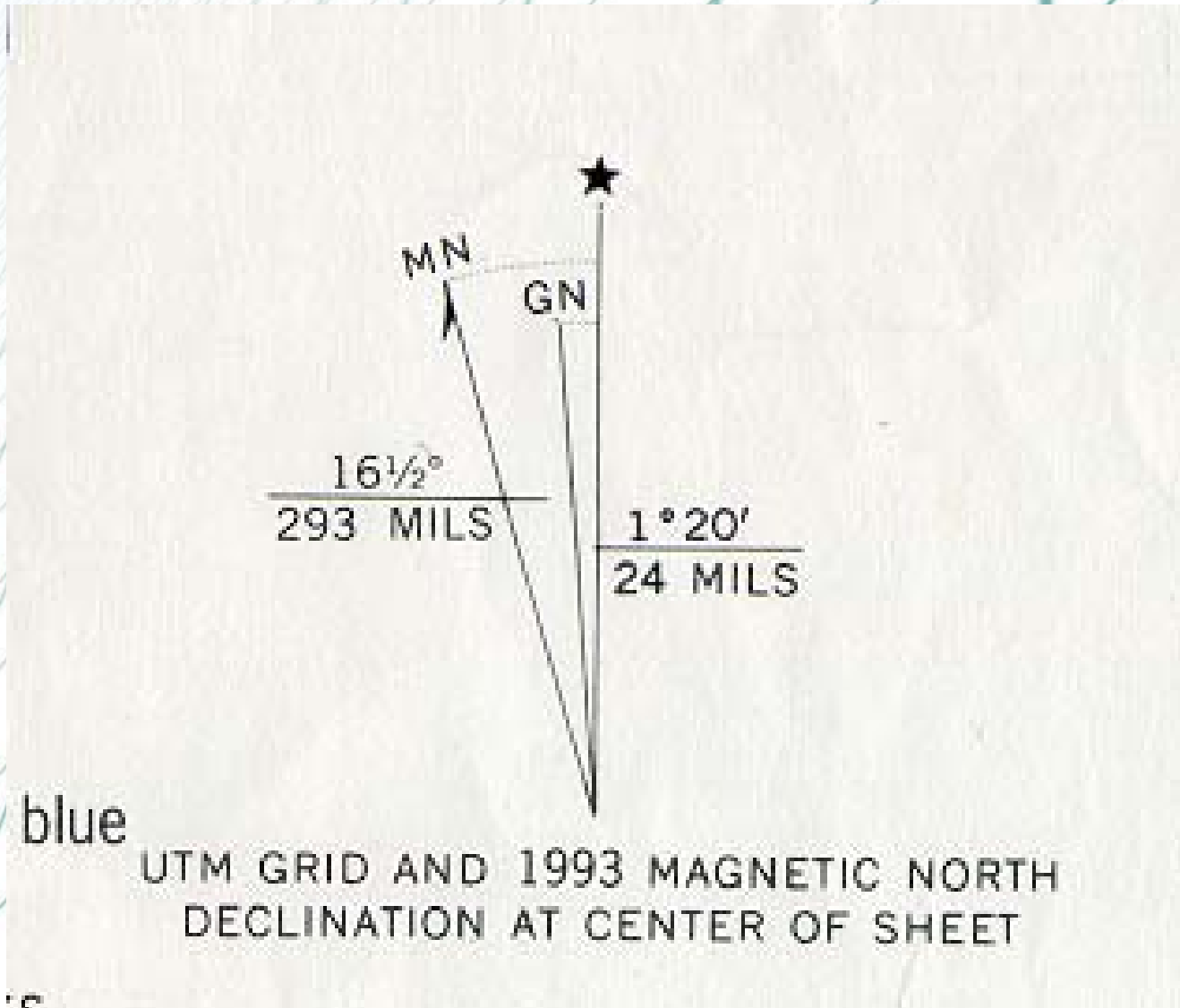
The background features a series of teal-colored lines that create a perspective effect, appearing to recede into the distance from the bottom left towards the top right. The lines vary in thickness and are set against a white background.

FIVE NORTHS

FIVE NORTHS

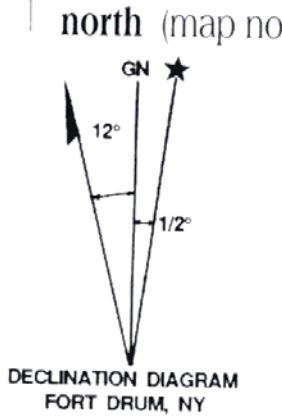
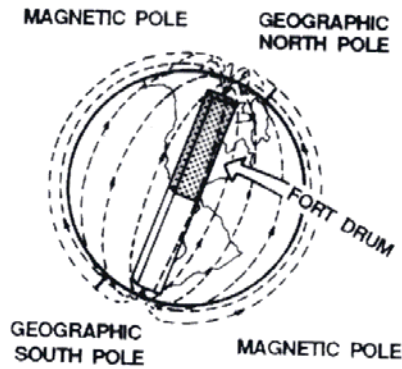
1. Astronomic North
Based on Earth's Rotation Axis
2. Geodetic North
Based on Ellipsoid's Rotation Axis
3. Grid North
Based in Central Meridian of System
4. Magnetic North
Based on magnetic lines of force
5. Assumed North
Based on any convenient axis

Geodetic –Grid –Magnetic North



Other Map Information: Norths

Coordinate



TRUE NORTH



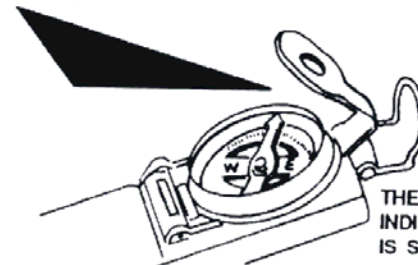
THE DIRECTION FROM ANY POSITION ON THE EARTH'S SURFACE TO THE NORTH POLE. ALL LINES OF LONGITUDE ARE TRUE NORTH LINES. THIS REFERENCE POINT IS SYMBOLIZED BY A STAR.

GRID NORTH



THE NORTH THAT IS ESTABLISHED BY THE VERTICAL GRID LINES ON THE MAP. THIS REFERENCE POINT IS SYMBOLIZED BY THE LETTERS GN.

MAGNETIC NORTH

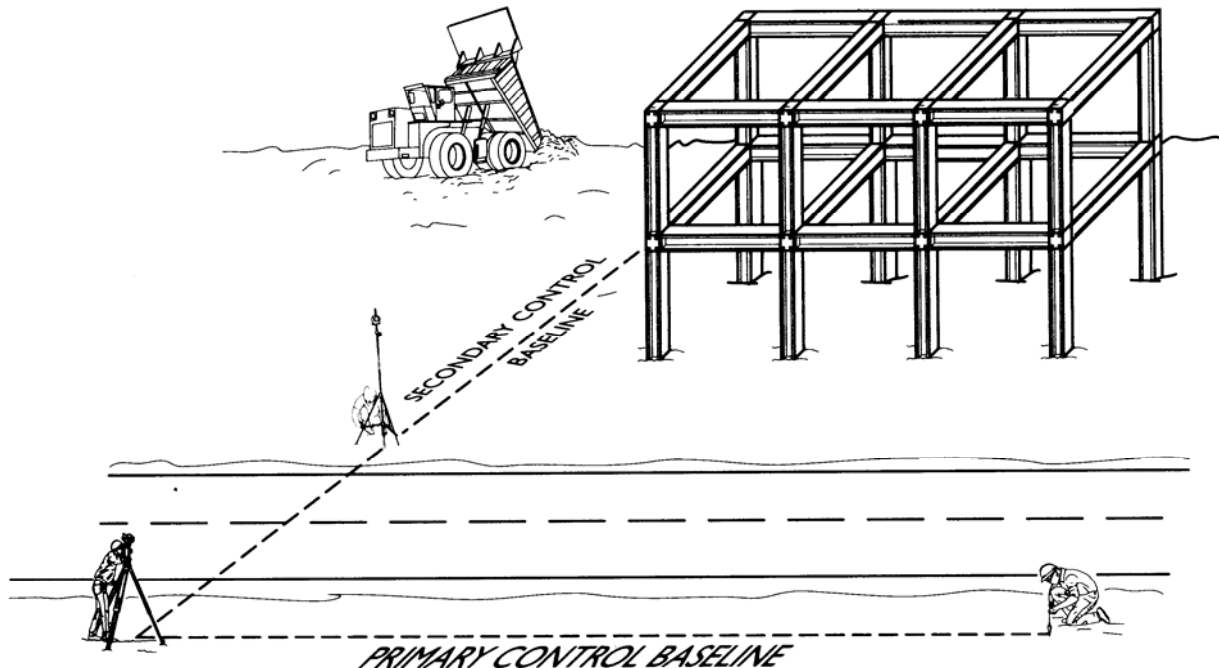


THE DIRECTION OF THE NORTH MAGNETIC POLE IS INDICATED BY A COMPASS. THIS REFERENCE POINT IS SYMBOLIZED BY A HALF ARROWHEAD.

Assumed North

Assumed Coordinate System

Using any arbitrary direction (Building column line, center of pipeline, etc.) as a reference meridian from which directions (angles) will be measured.



RECAP OF PRESENTATION OUTLINE

- 4 SURFACES
- 3 HEIGHTS
- 2 DATUMS
- 4 COORDINATE SYSTEMS
- 3 DISTANCES
- 5 NORTHS

RECOMMENDED SYSTEM TO USE FOR MUNICIPAL BOUNDS

N.H. STATE PLANE COORDINATES, NAD 83
(FEET OR METERS)

OR

LATITUDE(ϕ), LONGITUDE (λ), NAD 83